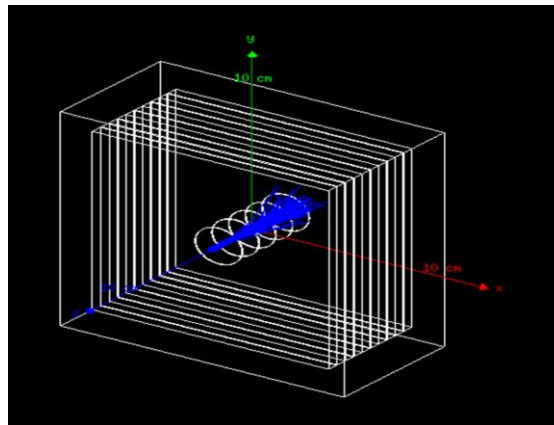


# *Fundamental Physics and True Muonium Production*

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FPUA 2015, RIKEN



# *Contents*

1. *Fundamental Physics - Motivation - Muon problems and True Muonium*
2. *TM - properties the spectrum decay widths mimic the spectrum of positronium scaled by the mass ratio*
3. *Frictional Cooling - principle and present status*
4. *Simulation - GEANT4*
5. *Proton Acc. LEAP-1 - Simulation POP-FRESH*
6. *Summary & Perspectives - Application - muon collider – MAP– neutrino factory*

- approach – routine 通例
- break through 開拓
- research direction 創作
- follow Dirac's way 新奇
- large-number-hypothesis 大胆
- fine structure constant (?) 精密

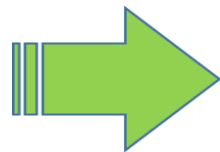


$10^{36}$

Y. Fujii , A. Iwamoto and H.Hidaka,  
appeared in BUTSURI 55(2000)

# *Verification of QED*

- Lamb shift of hydrogen  $2S_{1/2}-2P_{1/2} = 1057.86\pm 0.06$  MHz
- Fine structure  $2P_{3/2}-2P_{1/2} = 9911.38\pm 0.03$  MHz
- Hyperfine structure of hydrogen ground state  $\Delta\nu = 1420.4057517864(17)$  MHz
- Hyperfine structure of positronium  $\Delta\nu = (2.03396\pm 0.00005) \times 10^5$  MHz
- **Fine structure of muonium**  $\Delta\nu = 4463.311(12)$  MHz
- Anomalous magnetic moment of electron  $a_e = (1159.65218076\pm 27) \times 10^{-6}$
- **Anomalous magnetic moment of muon**  $a_\mu = (11659209\pm 6) \times 10^{-10}$
- Møller and Bhabha scattering – recoil effect in propagator



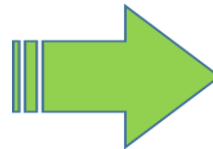
*Possibilities  
-New Physics-*

***Muon Problems(?)** : there are several discrepancies between experiment and theory in the *muon sector* (CODATA)*

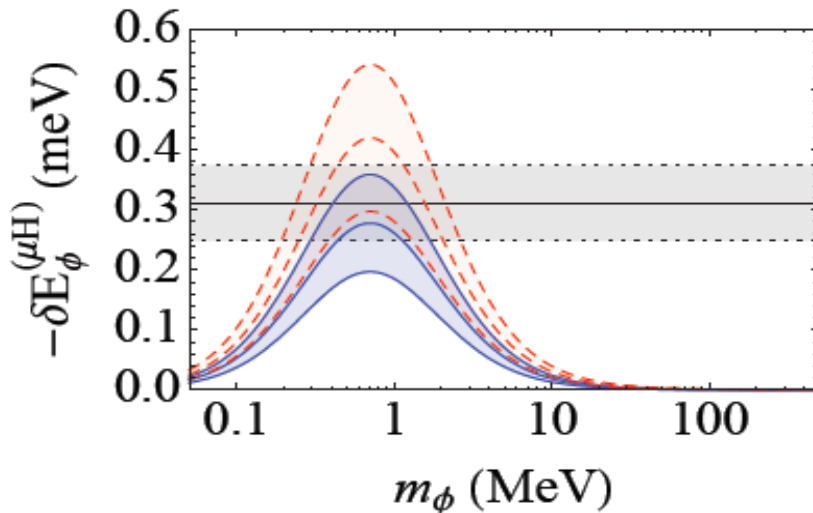
Experiments	Discrepancies	References
$a_\mu$	$2.9\sigma$	Phys. Rev D73
$r_p$	$7\sigma$	Science 339 Annals Phys. 331
$R_K B^+ \rightarrow K^+ \mu^+ \mu^-$	$2.6\sigma$	P.R.L. 113.15
$h \rightarrow \mu\tau$	$2.5\sigma$	CMS collab.

BSM ?  
EDM ?  
g-2 ?  
cLFV ?  
Dark matter ?  
Gravity ?  
Relativity ?

- present quest in high energy physics and astrophysics
- *models at hidden sector*
- mediator of a new force
- HPS 10 ~ 1000 MeV *assume a new mediator*



***Possibilities  
-New Physics-***



The contribution to the energy shift in  $\mu\text{H}$ , plotted against the mass of the mediator

- a new interaction between muons and protons in  $\mu\text{H}$
- Solid-blue, the theoretical deficit, scalar contribution to  $(g_\mu - 2) \sim$  upper and lower  $\pm 1$  s.d. away from the theoretical deficit.
- Solid-red, the vector contribution
- Coupling  $g_p = g_\mu$
- Solid horizontal, discrepancy between exp. and th. prediction assuming the CODATA

New physics; discrepancy between the CODATA value of the proton radius and the value deduced from the meas. of the Lamb shift in muonic hydrogen,

[ref.] Muonic hydrogen and MeV forces by David Tucker-Smith and Itay Yavin

assume a new mediator, the  
1<sup>st</sup> order perturbation  
theory

$$V_\phi(r) = (-)^{s+1} \left( \frac{g_\mu g_p}{e^2} \right) \frac{\alpha e^{-m_\phi r}}{r}$$

$$\begin{aligned} \delta E_\phi &= \int dr r^2 V_\phi(r) (|R_{20}(r)|^2 - |R_{21}(r)|^2) \\ &= (-)^{s+1} \frac{\alpha}{2a_\mu^3} \left( \frac{g_\mu g_p}{e^2} \right) \frac{f(a_\mu m_\phi)}{m_\phi^2} \end{aligned}$$

$$f(x) = x^4(1+x)^4, \quad a_\mu = (\alpha m_{\mu p})^{-1}$$

easy comparison

- $\delta E_p = \frac{2\alpha}{3n^3 a_\mu^3} \langle r_p^2 \rangle$
- $r_p$  is the proton radius and  
 $n=2$  is the principal quantum number

- Solid-blue , the theoretical deficit, scalar contribution to  $(g_\mu-2) \sim$  upper and lower  $\pm 1$  s.d. away from the th.deficit.
- Dashed-red, the vector contribution

assume a new mediator, the  
1<sup>st</sup> order perturbation  
theory

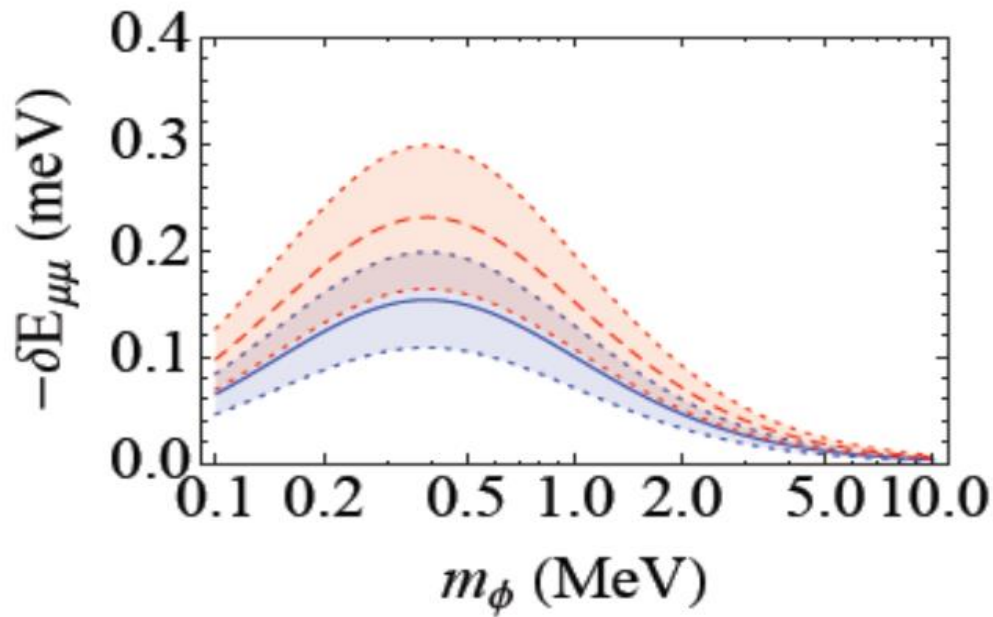
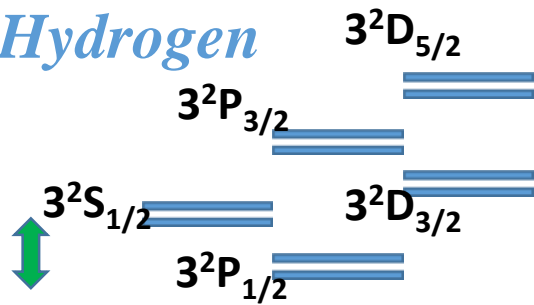


Fig. The contribution to the energy shift in TM as a function of the force carrier mass 2S-2P transition

# Hydrogen



pure leptonic atom

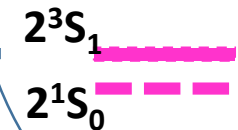
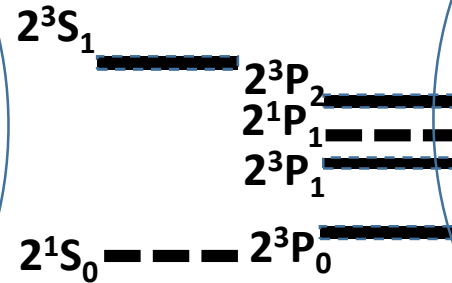
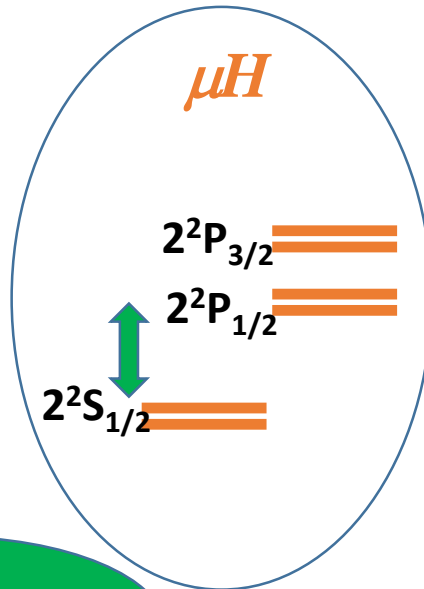
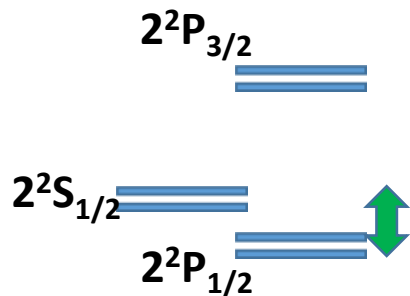
large reduced mass

$0.5 m_e$

$103.4 m_e$

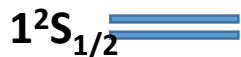
## Positronium

## True Muonium



Lamb shift

$n=2$  levels in muonic hydrogen, positronium and true muonium



$n = 3$  levels in hydrogen



True Muonium



# How do we produce *the true muonium* ?

- high energy

## Heavy Photon Search

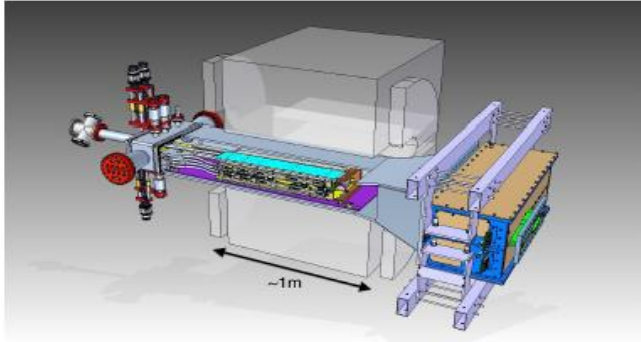


Figure: HPS Experiment at JLab

## Dimeson relativistic atom complex

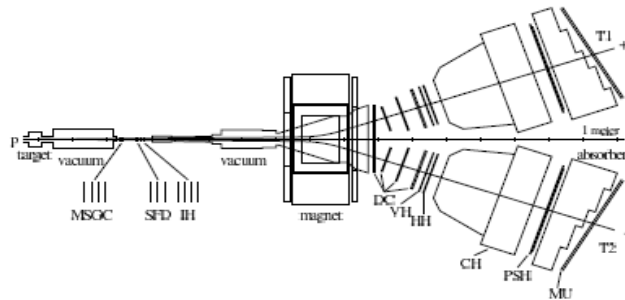
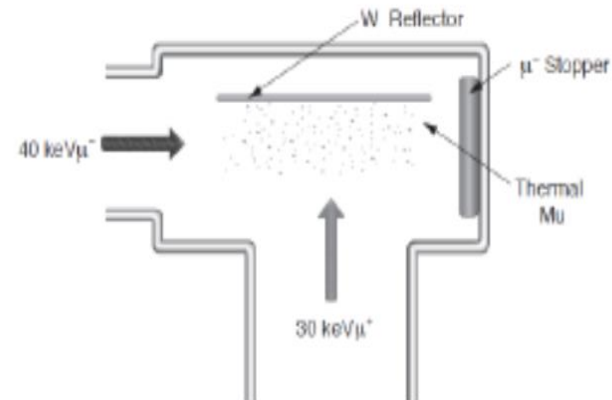
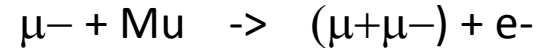


Figure: DIRAC Experiment at CERN

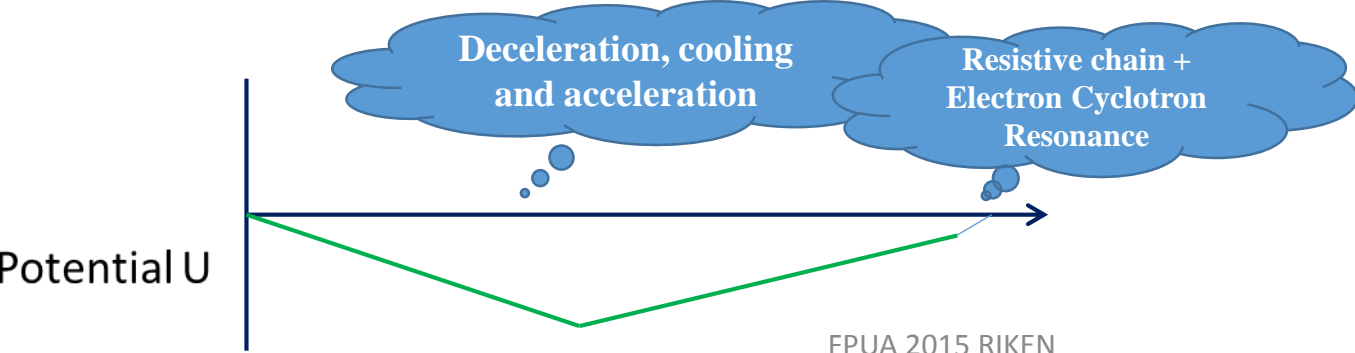
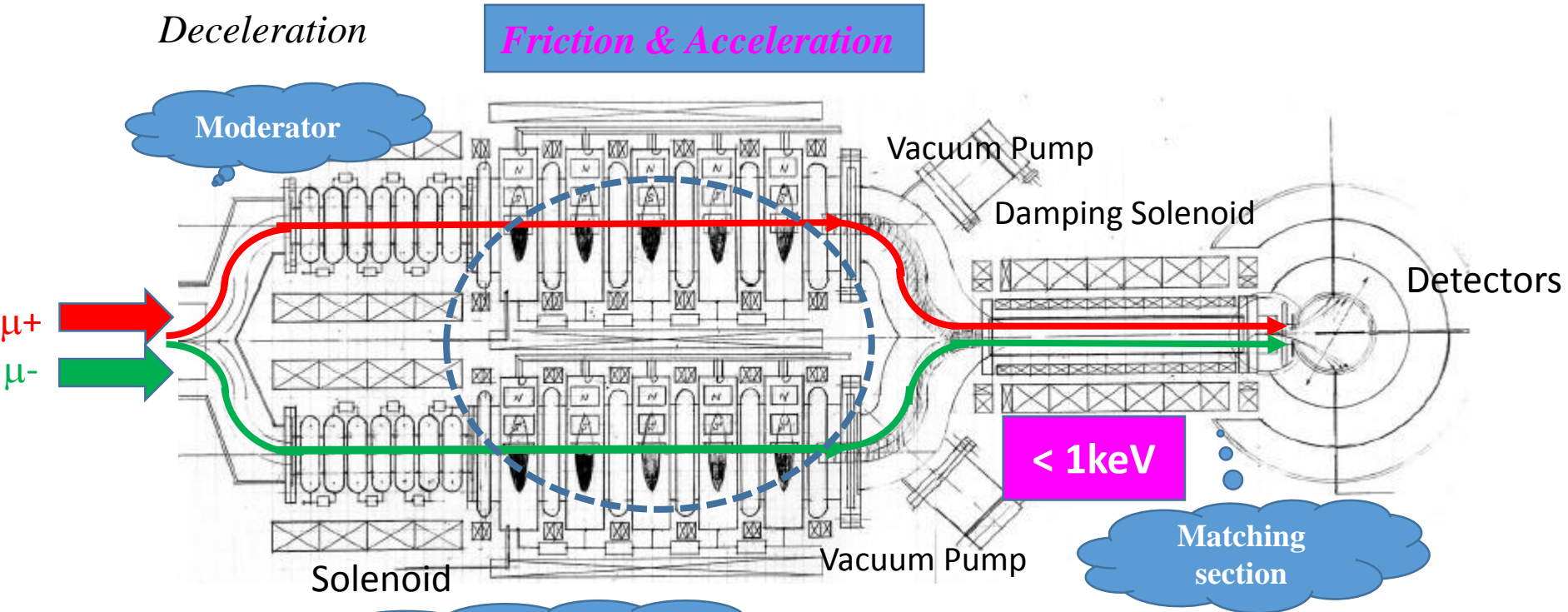
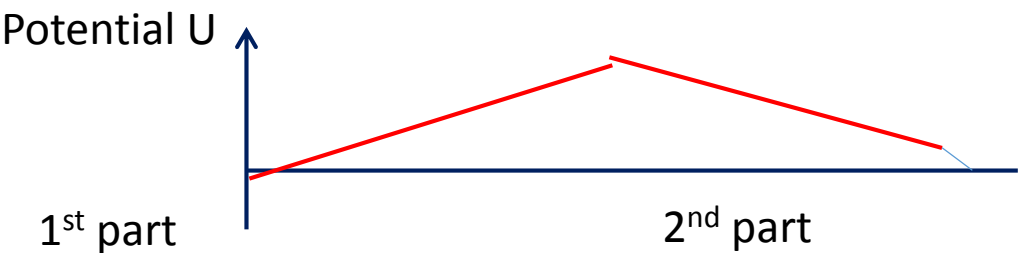
- low energy

## K. Nagamine

Possible experimental arrangements;  
detection of formation by K. Nagamine  
appeared in USM 2013 at Matsue



*low energy scheme*  
*almost the same procedures applied for  $\mu^+$  and  $\mu^-$*



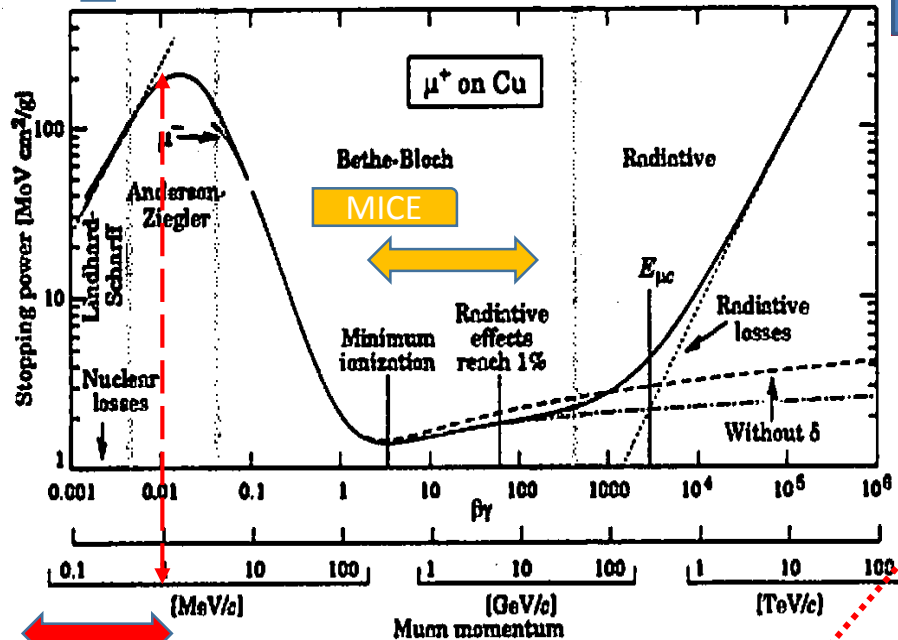
preliminary

Local density approx.  
for a free electron gas

Many electrons  
configuration in matter

Dielectric  
response

--Lindhard, Scharff (1954)



< 1 MeV/c

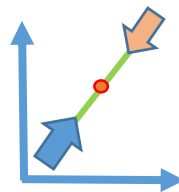
proportional to  $v$

Frictional cooling

Frictional force

$$\vec{F} = q (\vec{E} + \vec{v} \times \vec{B}) - \frac{dT}{ds} \hat{v}$$

$T$  is kinetic energy



Frictional cooling

GEANT4 program

LEAP 1  
exp.

Free electrons

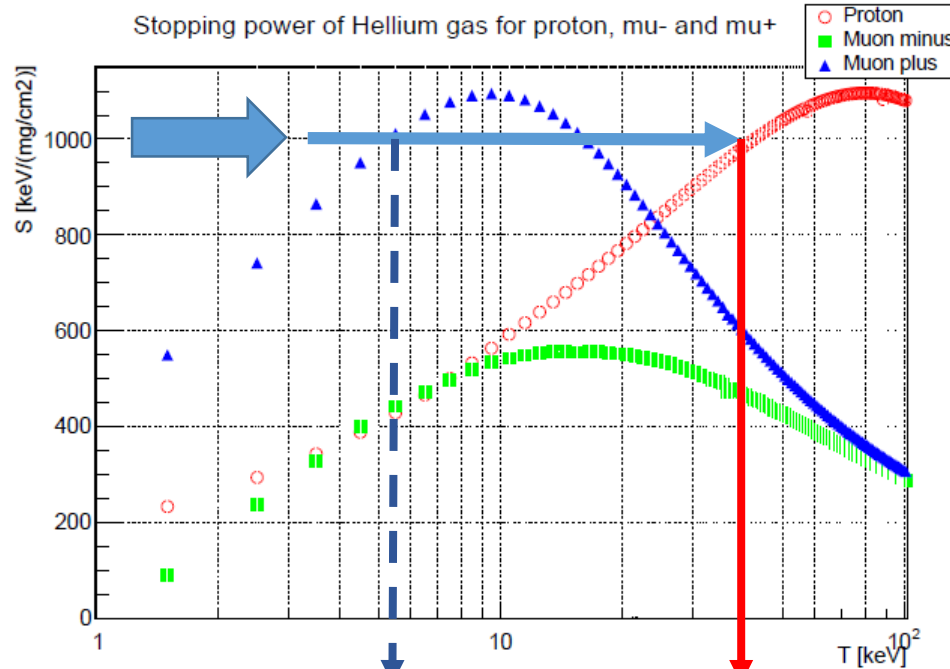
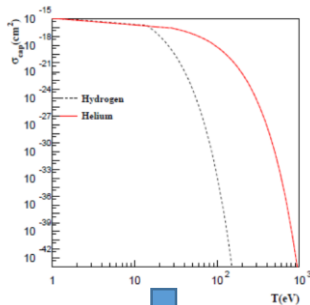
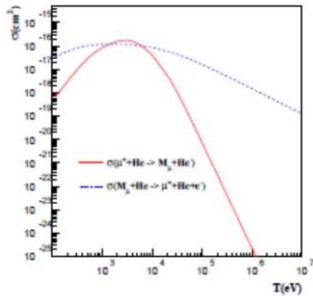
Frictional ECR Sheet – FRESH

Strategy for a true muonium production via  
a low energy collision with  $\mu^+$  and  $\mu^-$

## ➤ Strategy

# Energy region for frictional cooling of $\mu^+$ , $\mu^-$ and proton

Energy region of proton  
exp. → LEAP 1

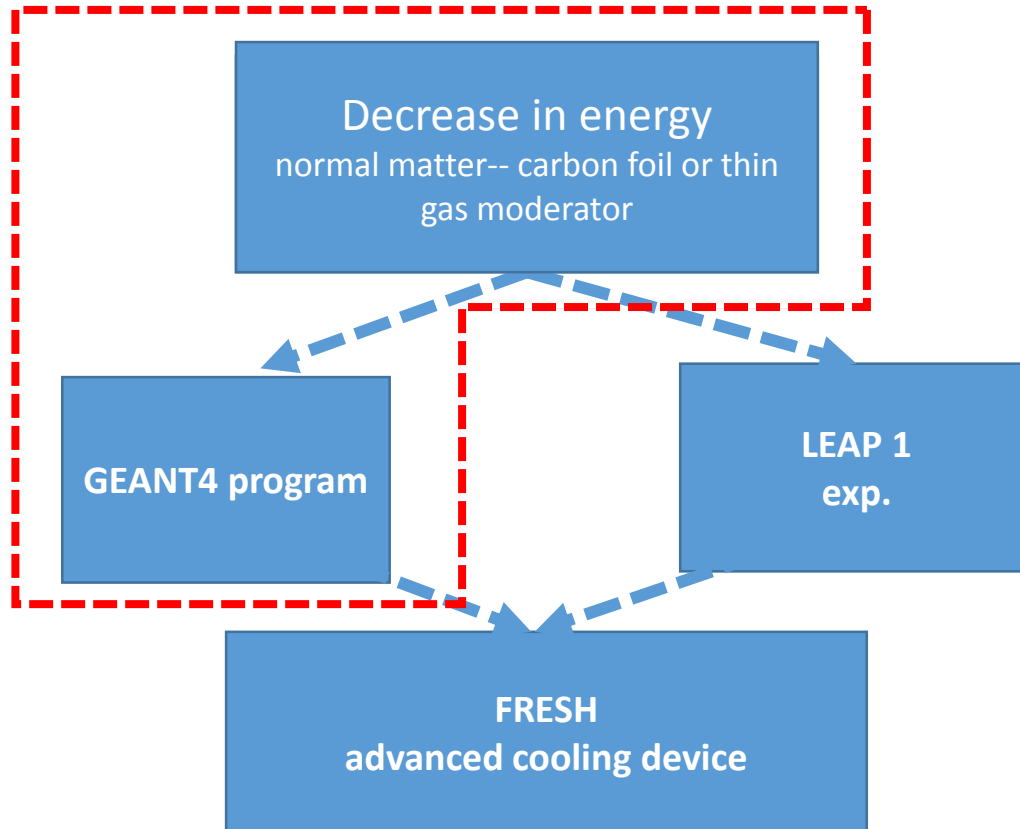


formation of few  
keV  $\mu^+$ ,  $\mu^-$

interesting energy  
region of proton

not so low,  
more than a  
few 10 eV

# I. Numerical simulation with GEANT4

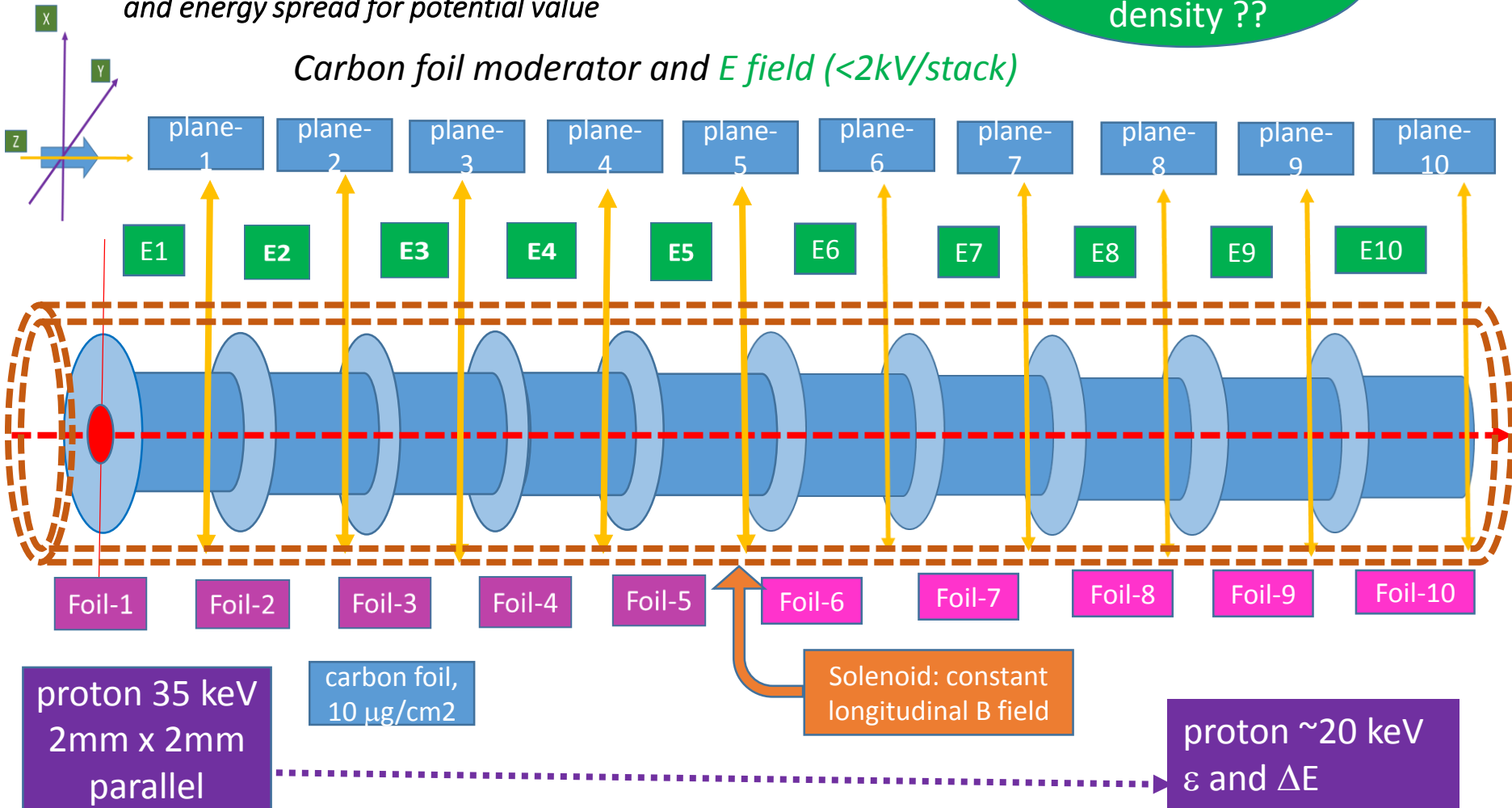


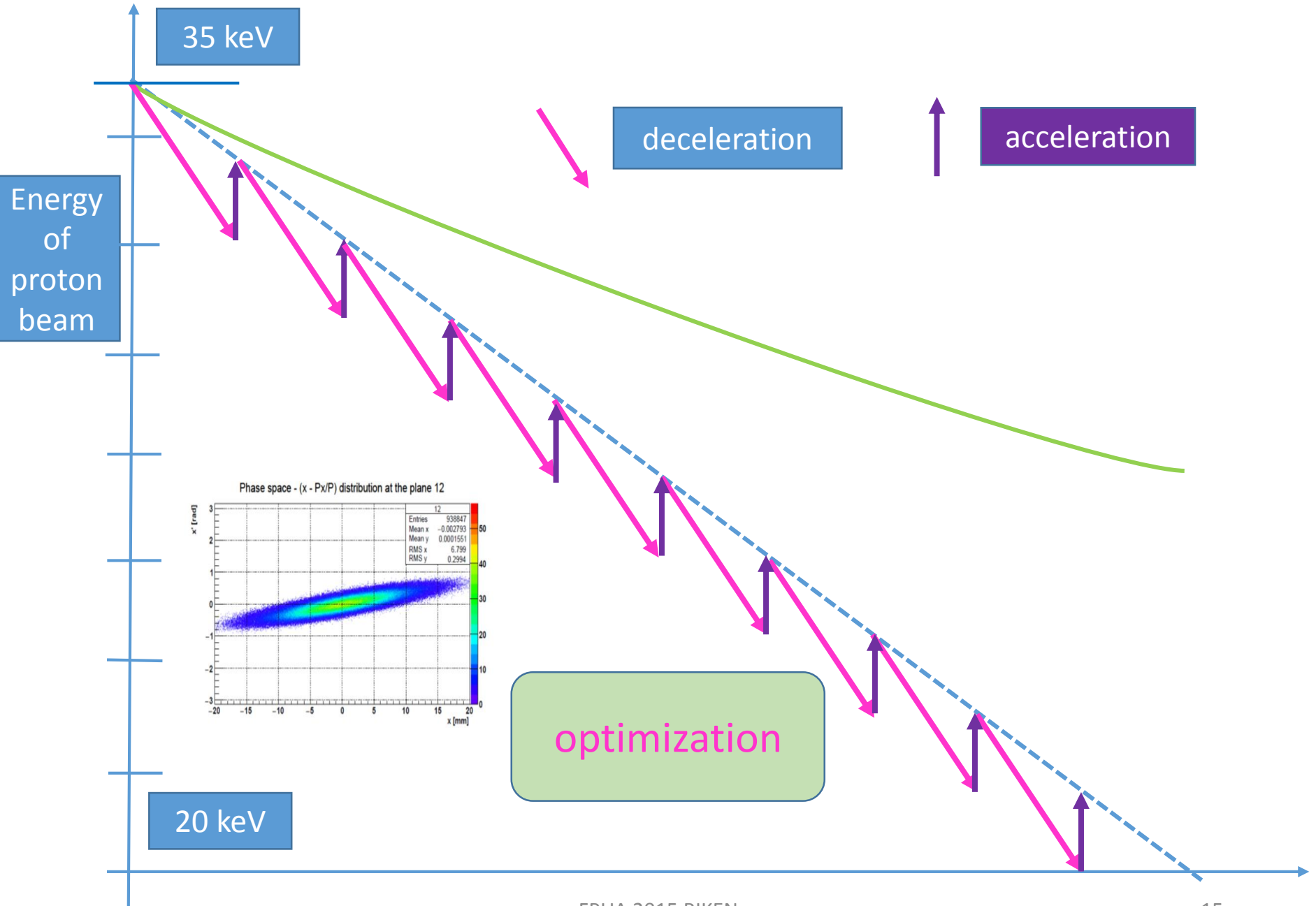
# GEANT4 Simulation

GEANT4 Simulation of proton beam emittance and energy spread for potential value

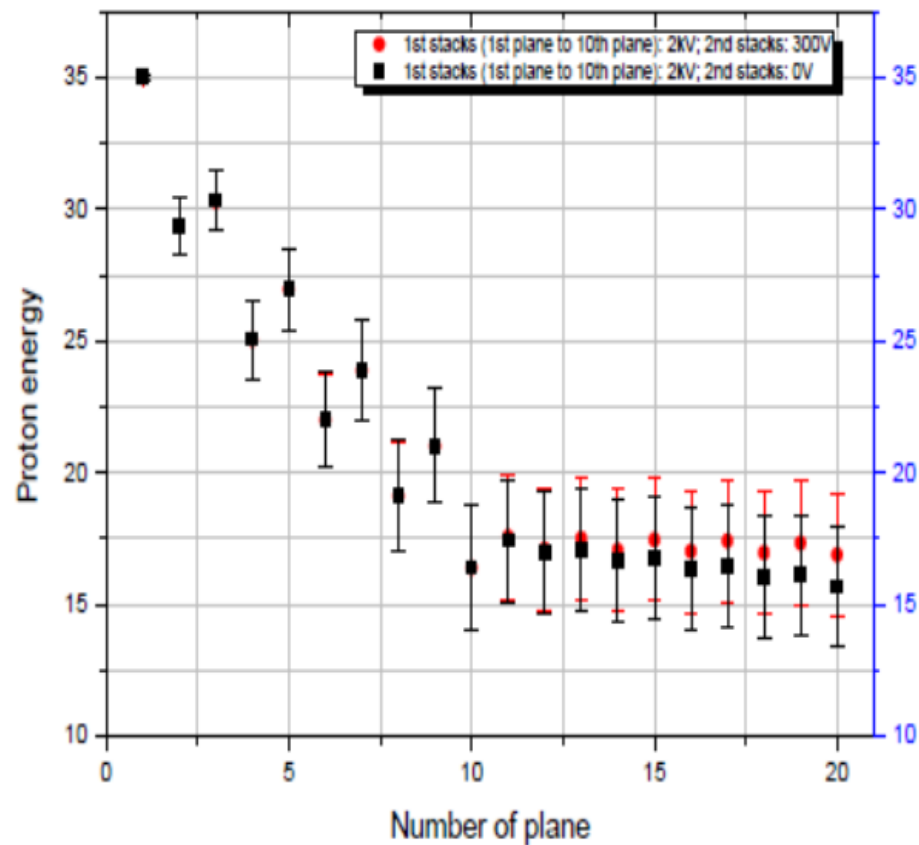
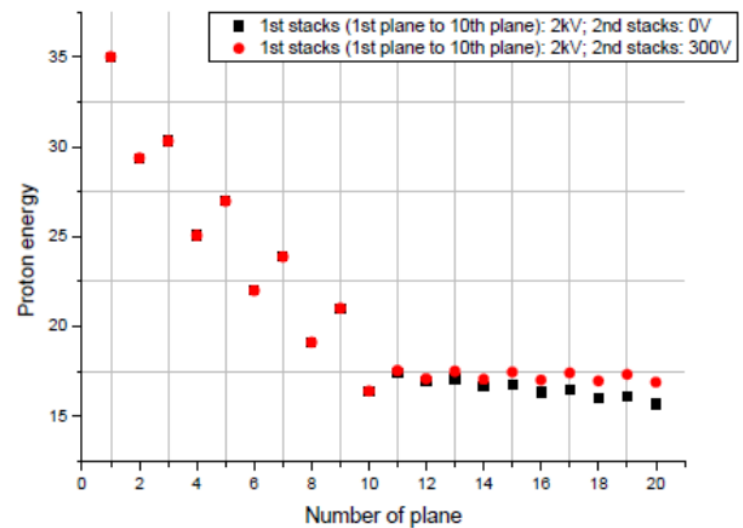
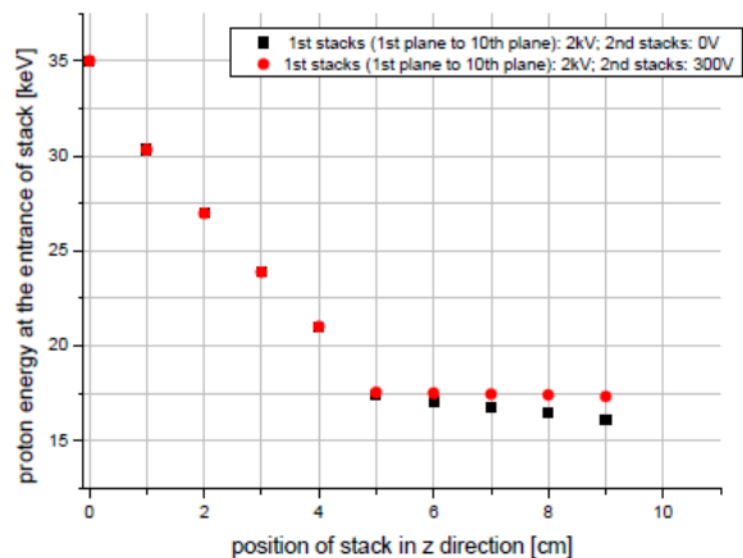
improve the phase space density ??

Carbon foil moderator and  $E$  field ( $< 2\text{ kV/stack}$ )





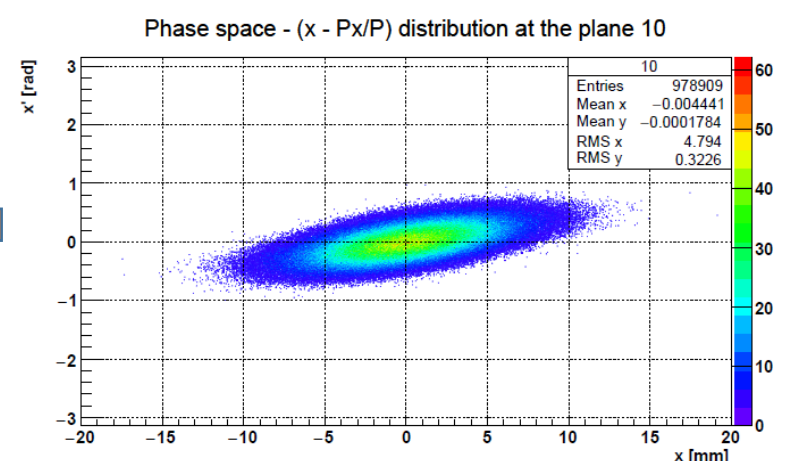
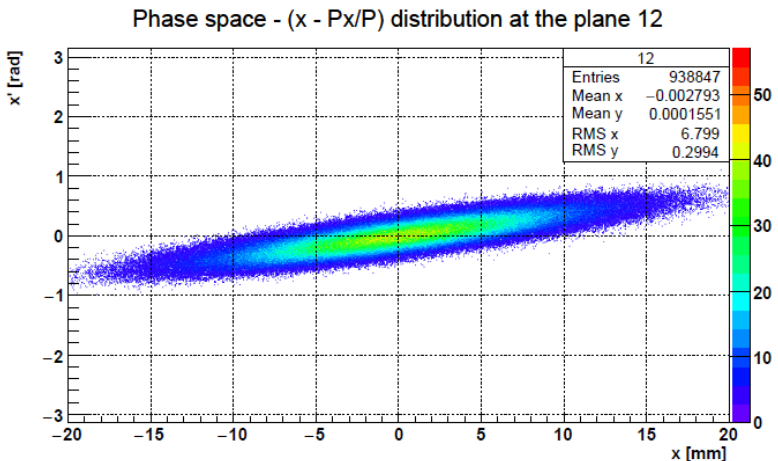
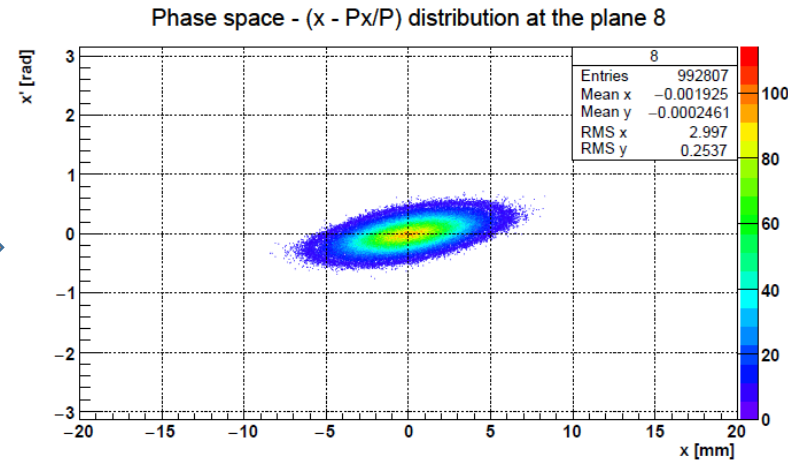
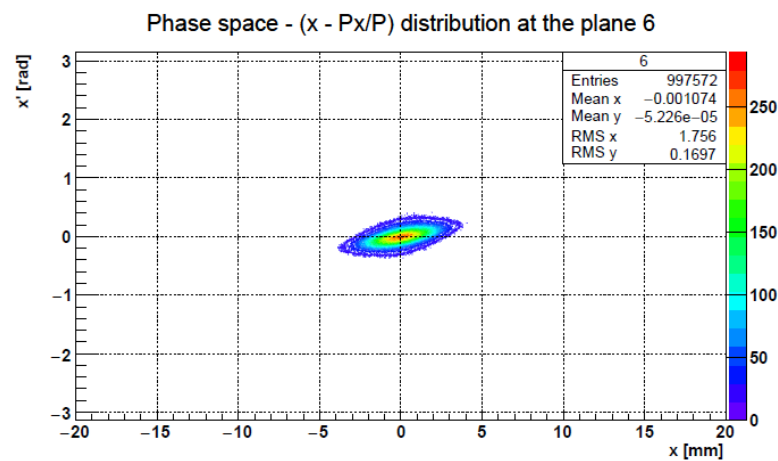
proton energy at  
each plane





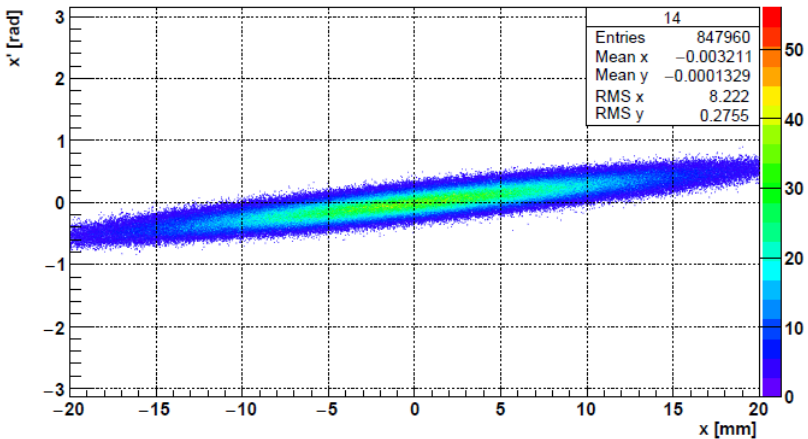
Several results

the 1st 5-stacks 2000 V and 2<sup>nd</sup> 5-stacks 300 V

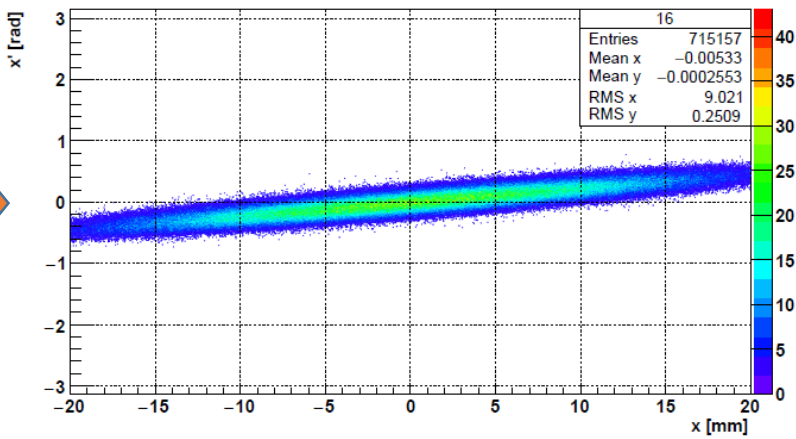


the 1st 5-stacks 2000 V and 2<sup>nd</sup>  
5-stacks 300 V

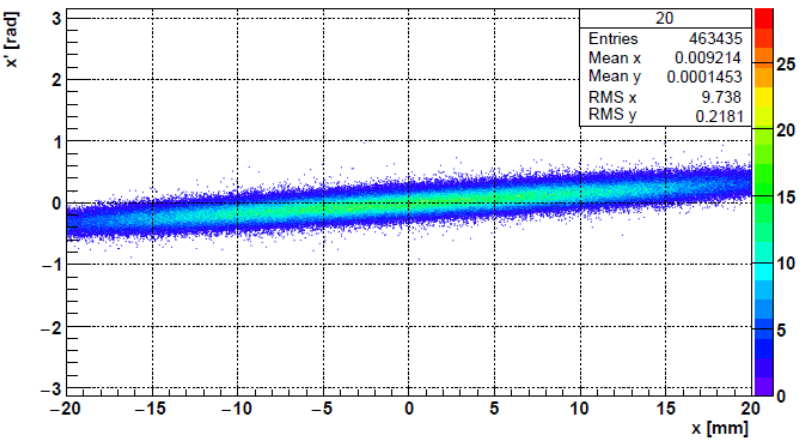
Phase space - (x - Px/P) distribution at the plane 14



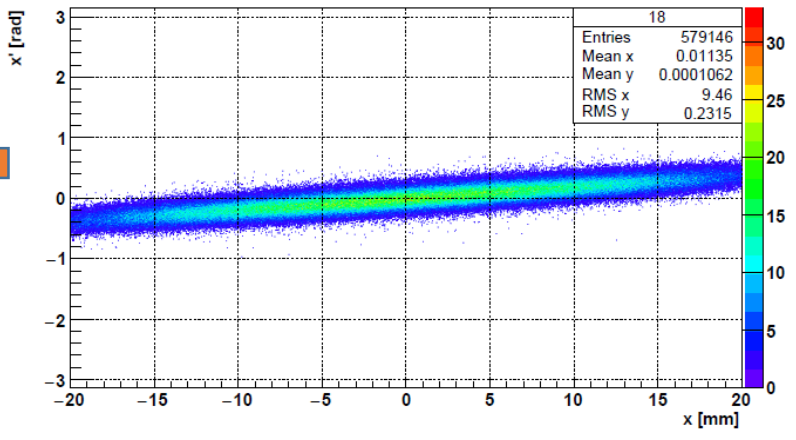
Phase space - (x - Px/P) distribution at the plane 16



Phase space - (x - Px/P) distribution at the plane 20



Phase space - (x - Px/P) distribution at the plane 18



# GEANT4 Simulation

2

29.37keV  
1.107keV

4

25.06keV  
1.501keV

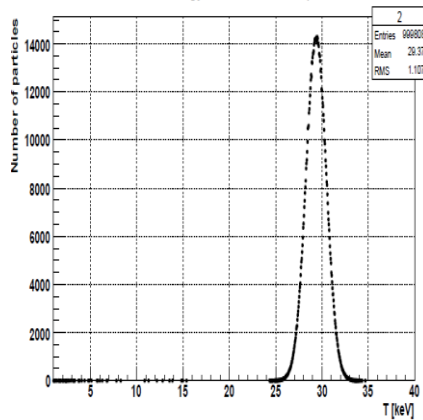
6

21.99keV  
1.787keV

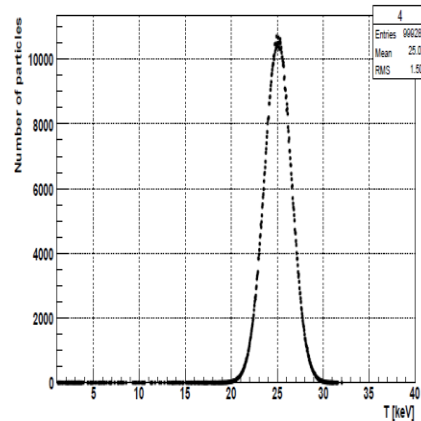
8

19.11keV  
2.091keV

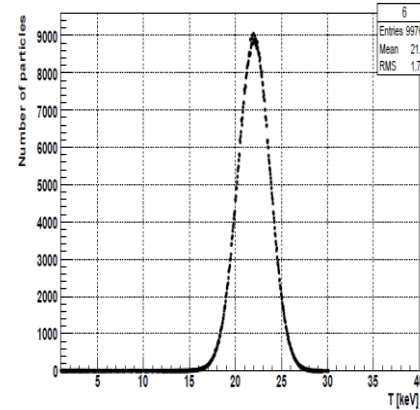
Proton energy distribution at the plane 2



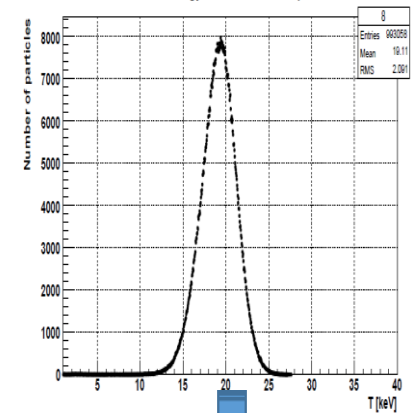
Proton energy distribution at the plane 4



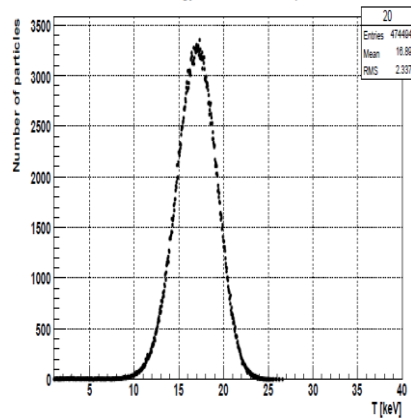
Proton energy distribution at the plane 6



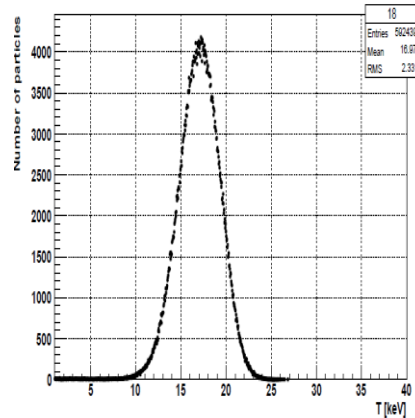
Proton energy distribution at the plane 8



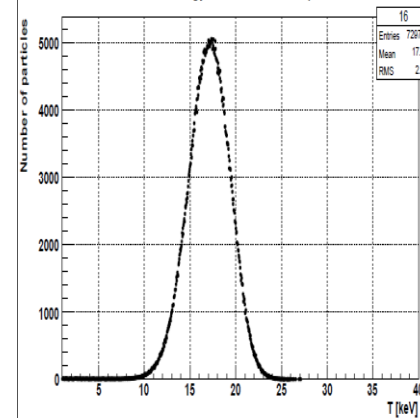
Proton energy distribution at the plane 20



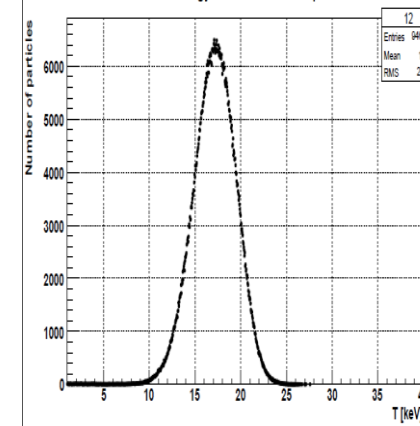
Proton energy distribution at the plane 18



Proton energy distribution at the plane 16



Proton energy distribution at the plane 12



16.39keV  
2.337keV

20

16.97keV  
2.337keV

18

17.02keV  
2.320keV

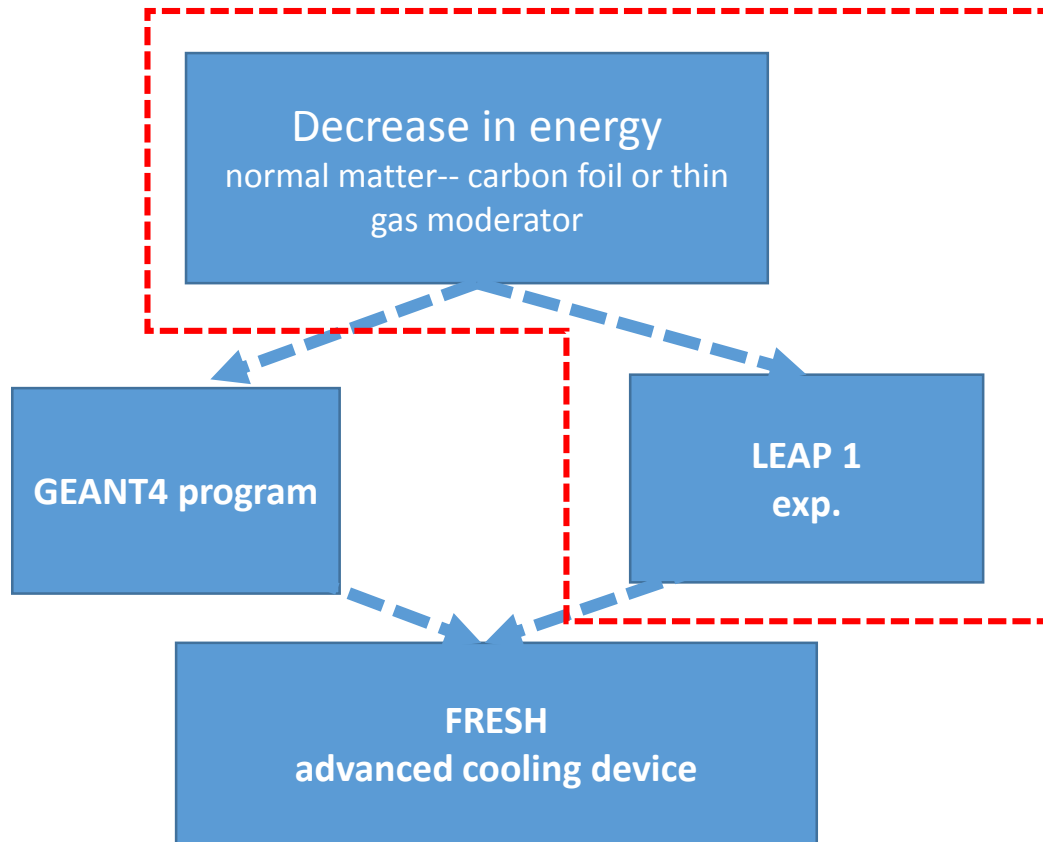
16

17.11keV  
2.345keV

12

19

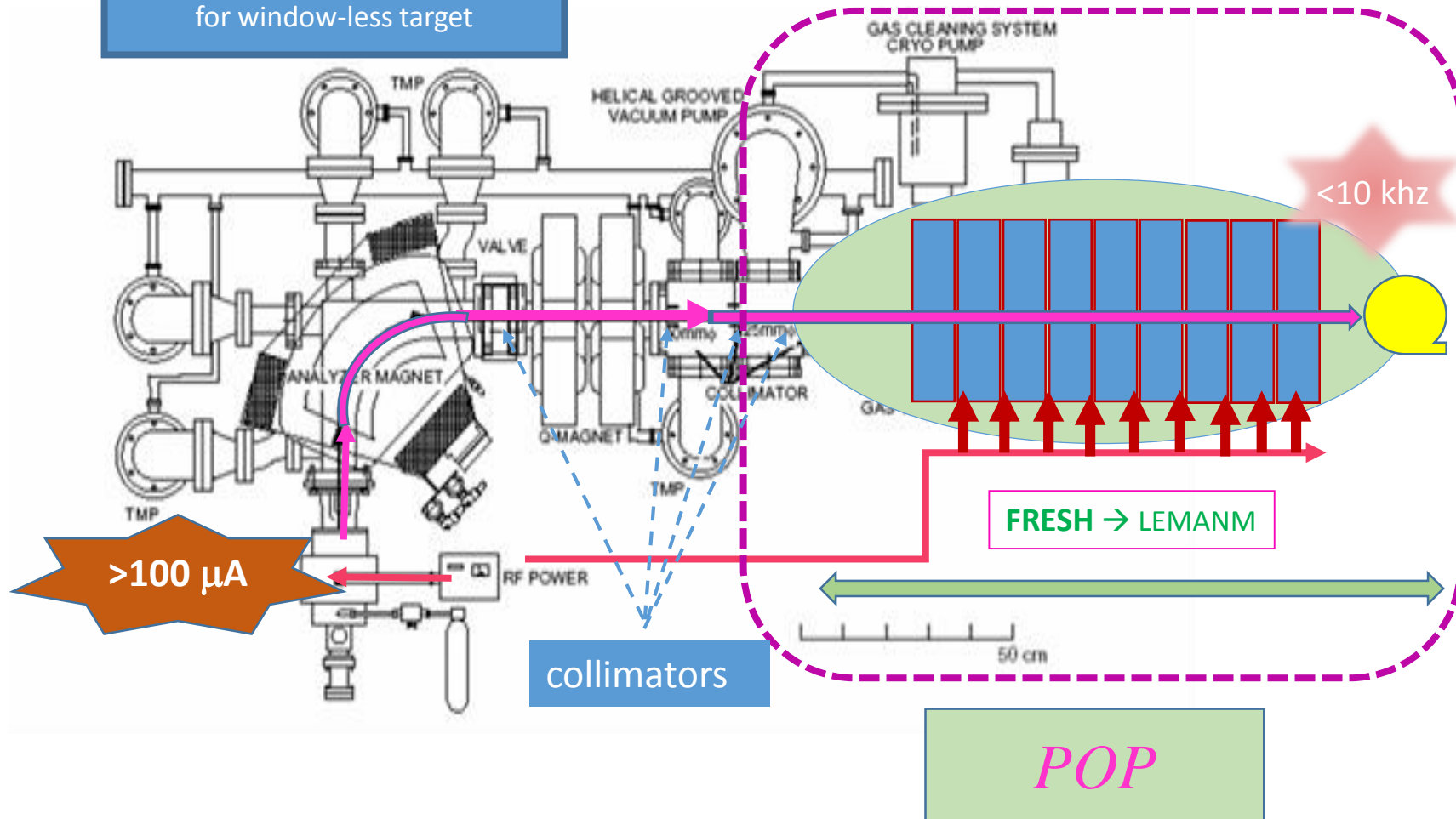
## II. Experimental *proof of principle* with proton beam



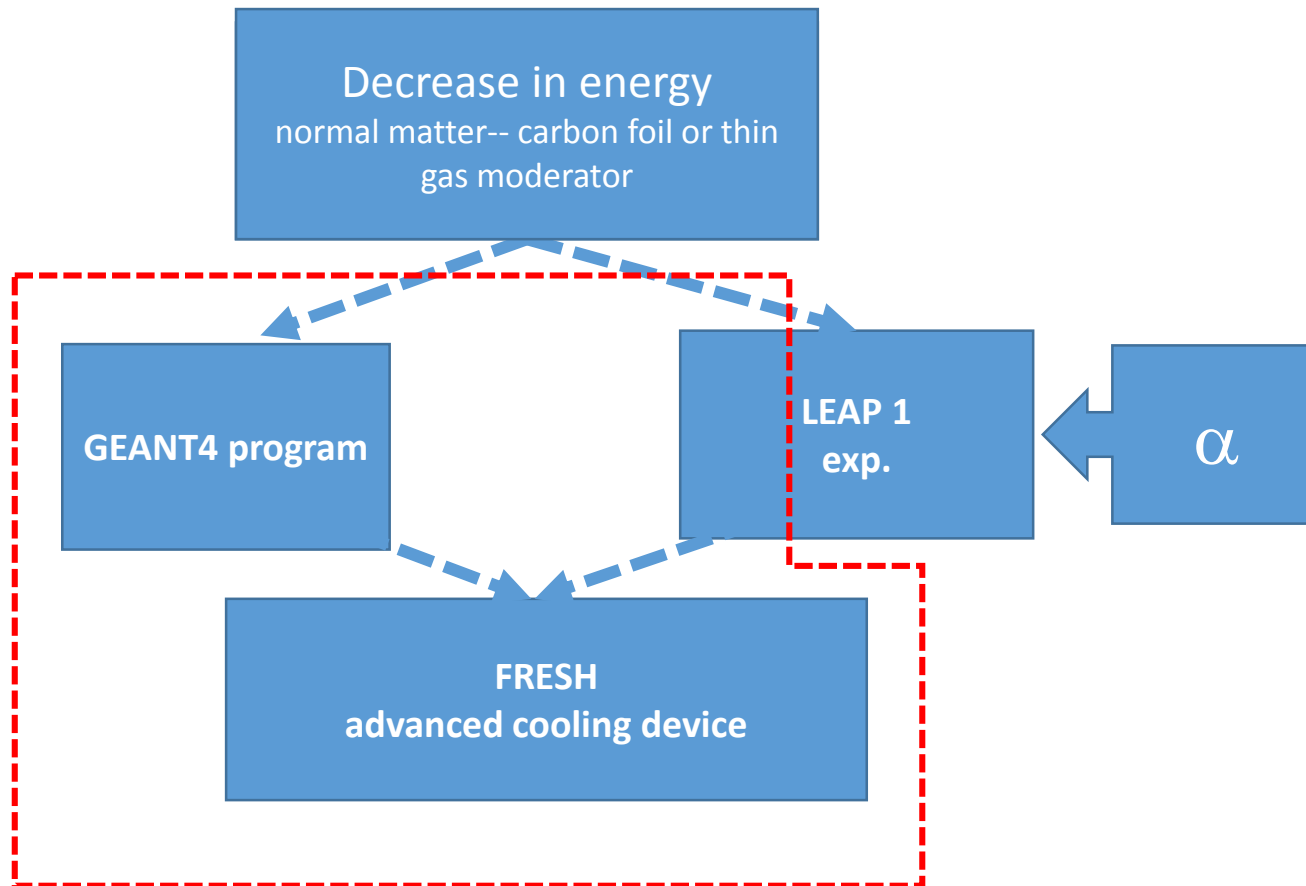
## II. Low Energy Accelerator Project ( LEAP 1 )

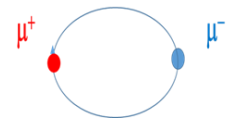
- Carbon foil
- Helium gas
- Hydrogen gas
- ECR plasma

Differential pumping is available for window-less target



### III. *FRESH advanced cooling device*





**FRESH** – advanced frictional cooling device for muons

--frictional cooling with **ECR sheet**--



Proof of principle

➤ **F**Rictional **E**CR

**S**heet for muon cooling

- Plasma,  **$dE/dx$**  --larger stopping power
- Plasma, **density** --less matter
- Plasma, **conductivity** --apply potential to
- Plasma, **ionization** – bring another merit

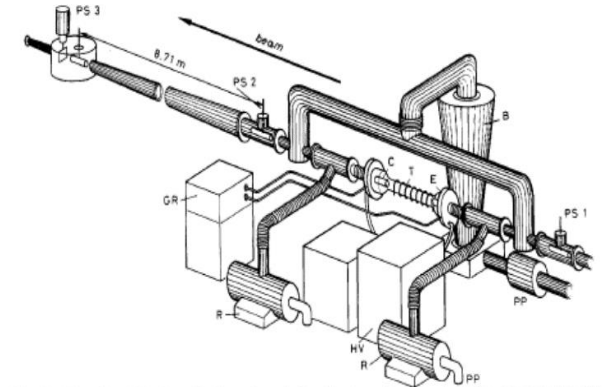
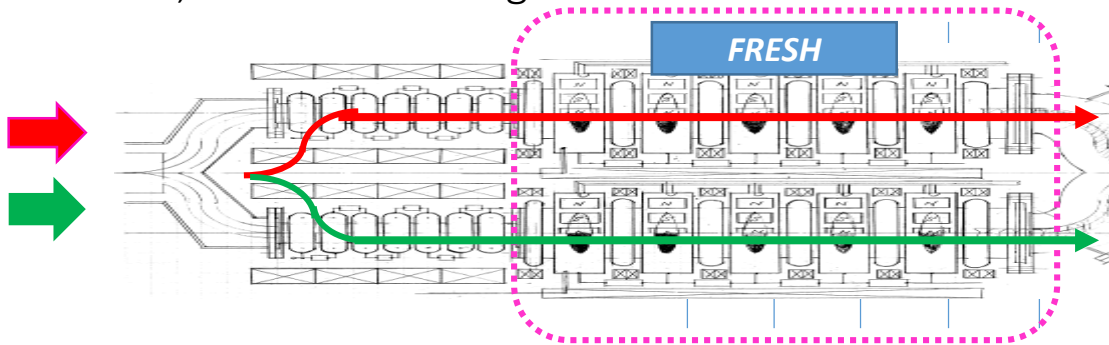
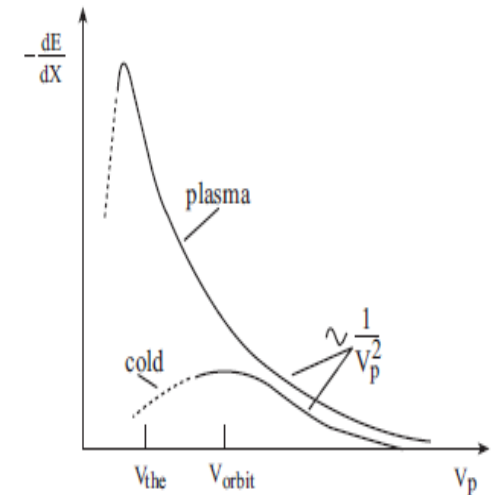


Fig. 1. - Experimental set-up. T: plasma target, C: collimators, E: electrodes, GR: gas regulation, HV: high-voltage supply, PP: primary pumps, R: roots, B: booster, PS1, 2, 3: phase probes.



Orsay and TIT exp.

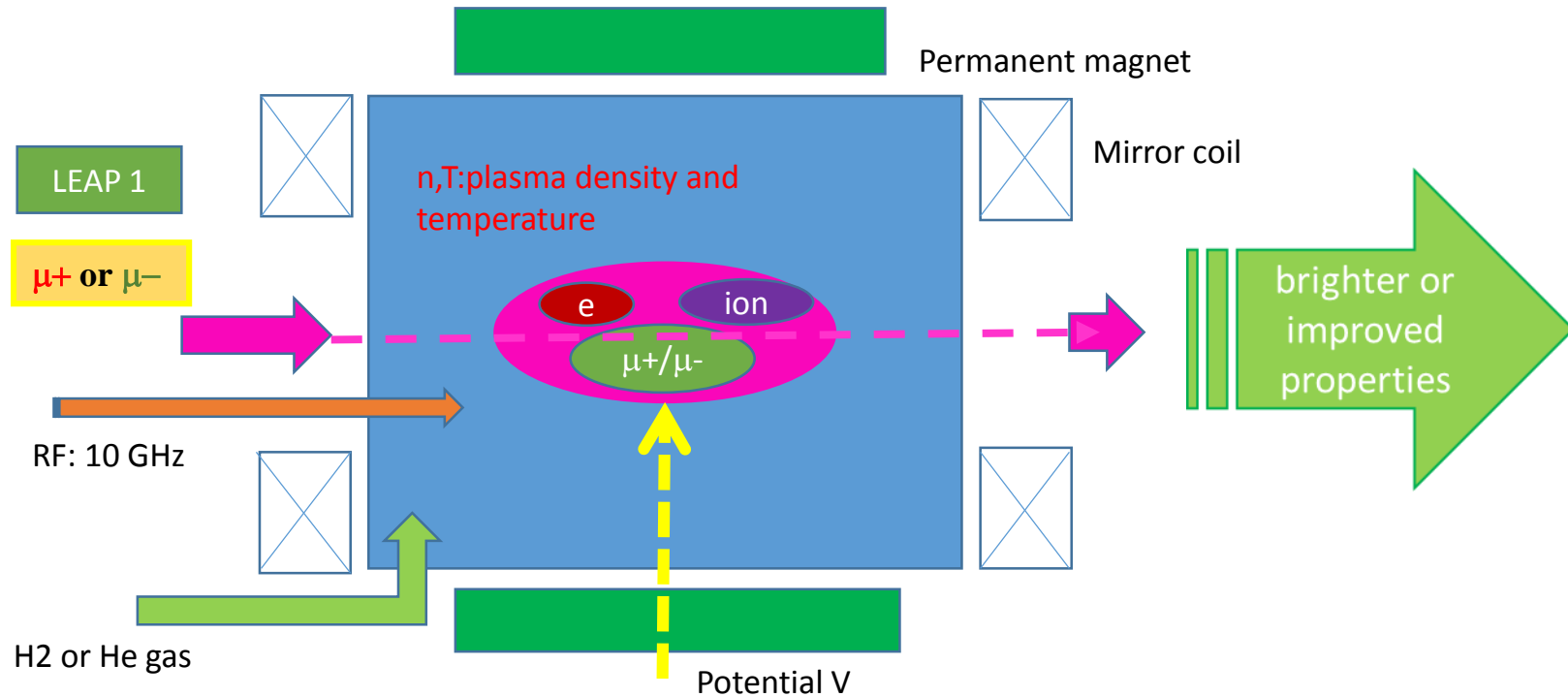
## ➤ Ideas

Atomic, molecular physics/chemistry  
and subatomic physics with exotic particles



### ***Basic Plasma physics, with proton, $\mu^+$ , $\mu^-$***


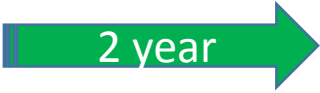
- absolute minimum B ECR <--- one example





➤ Low energy muons

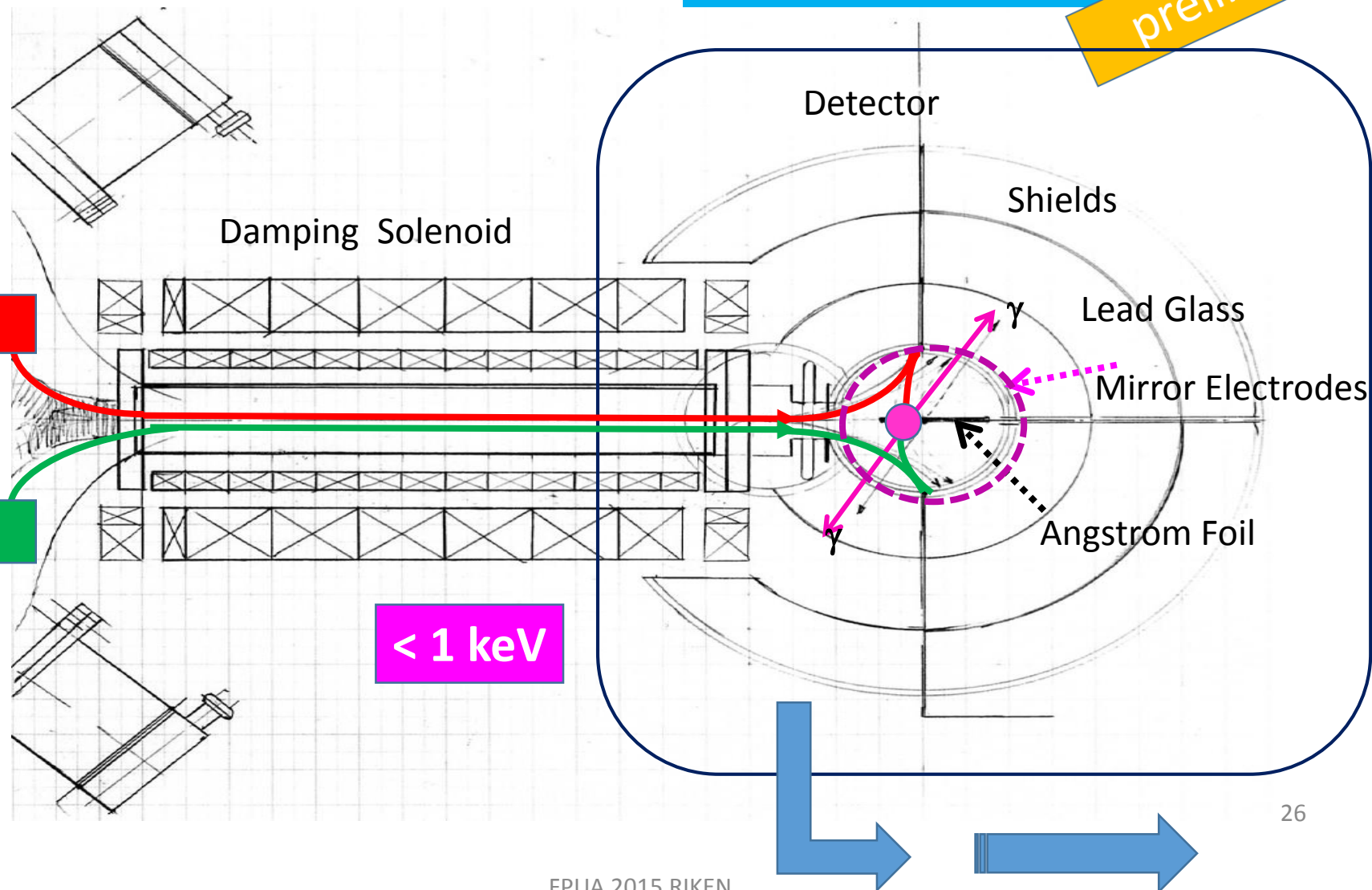
## IV. TM production and Experiments

	 1 year		
	proton	$\mu^+$	$\mu^-$
incident energy	~30 keV	expect a few keV	> ~10 keV
beam quality	uniform or Gaussian	uniform or Gaussian	uniform or Gaussian
moderator	Carbon + Helium, H <sub>2</sub>	Helium	Helium or Hydrogen
gas moderator (nominal)	0.1 Torr (plasma)	0.1 Torr (plasma)	0.1 Torr (plasma)
potential $\Delta U$	1~2 kV	~100 V	~100 V
stack numbers	5 stacks—10 stacks	5 stacks	10 stacks
final energy T	~10 keV	a few keV, <1keV	a few keV, <1 keV
density increase in $\epsilon$	xxxxxx	xxxxxx	xxxxxx
loss actor	xxxxxx	xxxxxx	xxxxxx

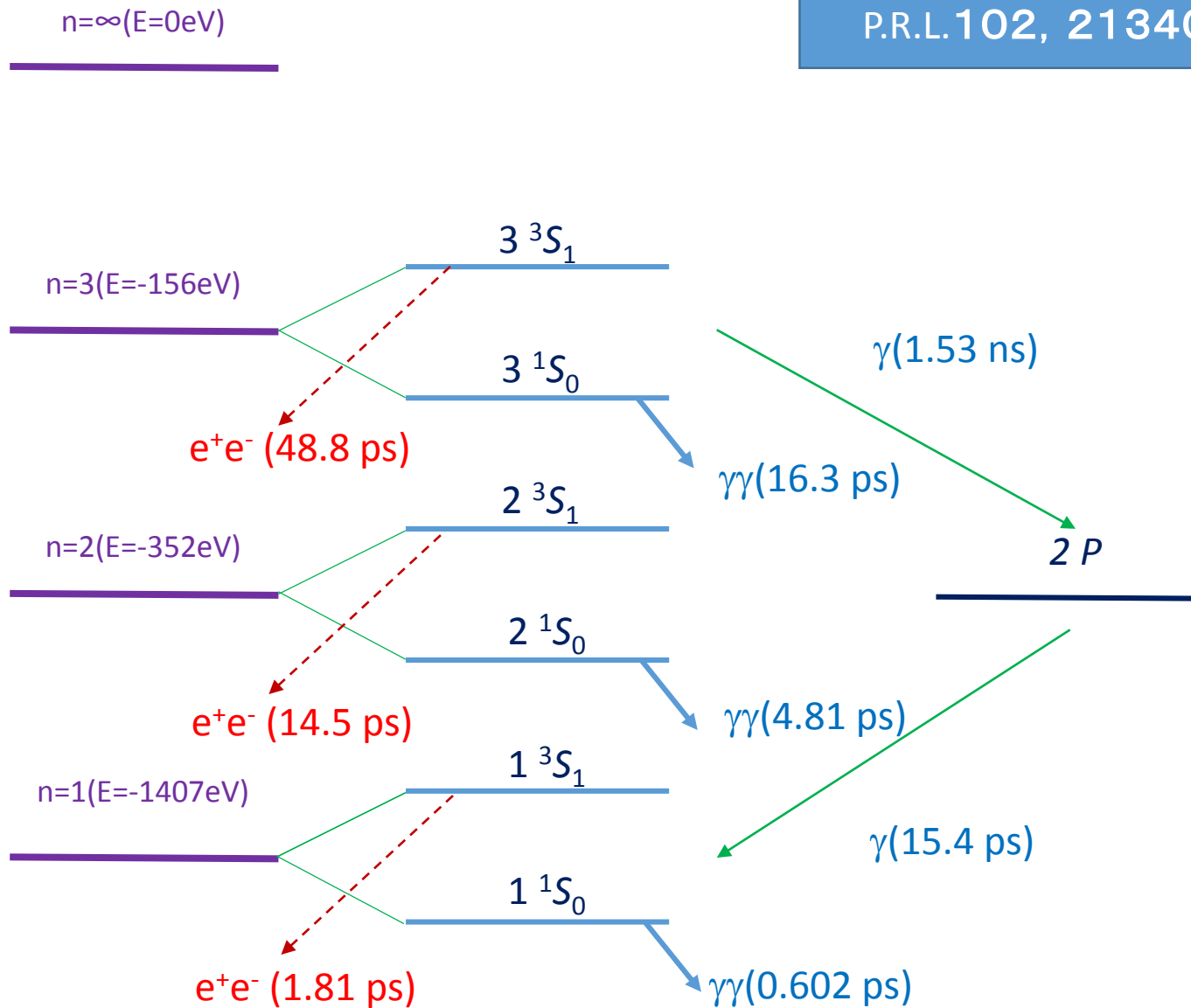


## Production & Detection

preliminary



True muonium level diagram  
P.R.L.102, 213401 (2009)



# Summary (要約)

- *quests of several physics interests in TM (探求)*
- *traditional and new physics (伝統)*
- *fine structure, hyperfine structure, Lamb Shift (手順)*
- *strategy of production for TM (革新)*
- *frictional cooling (開拓)*
- *POP facility and simulation study (実行)*
- *FRESH device (創作)*
- *perspectives (飛躍)*