

Time-Reversal Invariance Violation in Nuclei

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(FPUA)

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Sakharov Criteria (JETP Lett. 5, 32 (1967))

Particle Physics can produce matter/antimatter asymmetry in the early universe *IF* there is:

- Baryon Number Violation
 - CP & C violation
 - Departure from Thermal Equilibrium
- ➔ **TRIV**

According to our hypothesis, the occurrence of C asymmetry is the consequence of violation of CP invariance in the nonstationary expansion of the hot universe during the superdense stage, as manifest in the difference between the partial probabilities of the charge-conjugate reactions. This effect has not yet been observed experimentally, but its existence is theoretically undisputed (the first concrete example, Σ_+ and Σ_- decay, was pointed out by S. Okubo as early as in 1958) and should, in our opinion, have an important cosmological significance.



Observed:

$$(n_B - n_{\bar{B}}) / n_\gamma \simeq 6 \times 10^{-10}$$

(WMAP+COBE,2003)

SM prediction:

$$(n_B - n_{\bar{B}}) / n_\gamma \sim 6 \times 10^{-18}$$

Neutron EDM

Only \vec{s} : $(\vec{s} \sim [\vec{r} \times \vec{p}])$

if $\exists \vec{d}_n = e \cdot \vec{r}$

\mathcal{P} : $\vec{s} \rightarrow +\vec{s}; \quad \vec{r} \rightarrow -\vec{r};$

\mathcal{T} : $\vec{s} \rightarrow -\vec{s}; \quad \vec{r} \rightarrow +\vec{r};$

$\Rightarrow \vec{d}_n = \vec{0}$

A formal approach

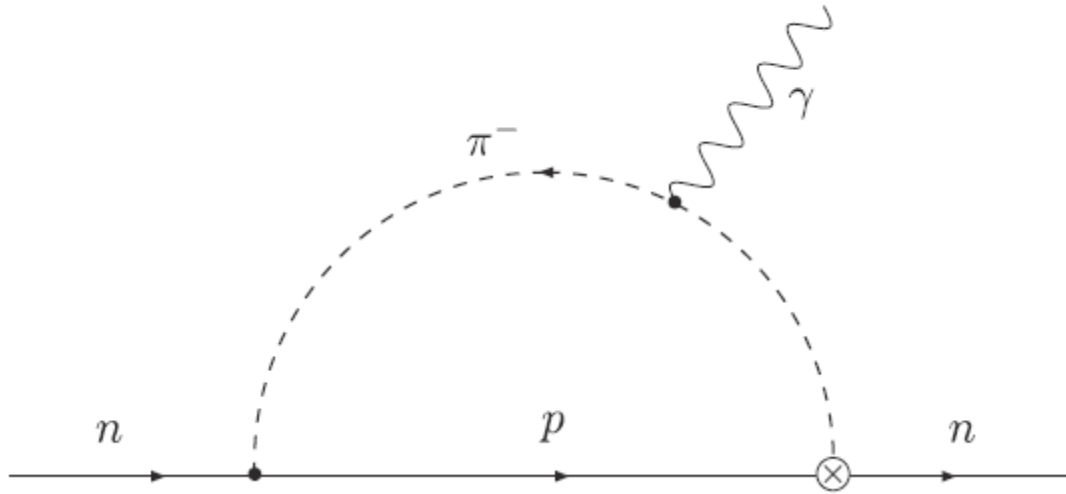
$$\langle p' | J_\mu^{em} | p \rangle = e \bar{u}(p') \left\{ \gamma_\mu F_1(q^2) + \frac{i\sigma_{\mu\nu} q^\nu}{2M} F_2(q^2) - G(q^2) \sigma_{\mu\nu} \gamma_5 q^\nu + \dots \right\} u(p)$$

$$q^\nu = (p' - p)^\nu; \quad \sigma_{\mu\nu} = \frac{i}{2} [\gamma_\mu, \gamma_\nu]; \quad \gamma_5 = \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$$

$$G(0) = d$$

$$H_{EDM} = i \frac{d}{2} \bar{u} \sigma_{\mu\nu} \gamma_5 u F^{\mu\nu} \rightarrow -(\vec{d} \cdot \vec{E})$$

Chiral Limit



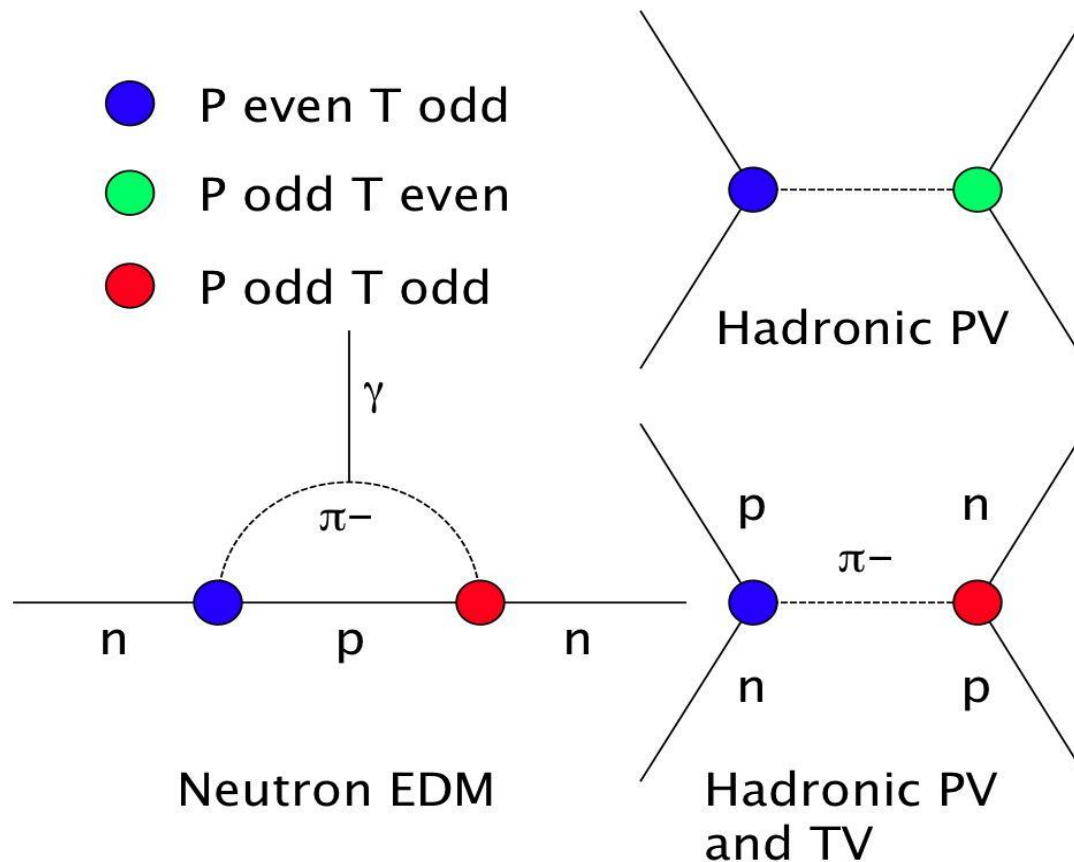
$$d_n = -d_p = \frac{e}{m_N} \frac{g_\pi (\bar{g}_\pi^{(0)} - \bar{g}_\pi^{(2)})}{4\pi^2} \ln \frac{m_N}{m_\pi} \simeq 0.14 (\bar{g}_\pi^{(0)} - \bar{g}_\pi^{(2)})$$

With more details...

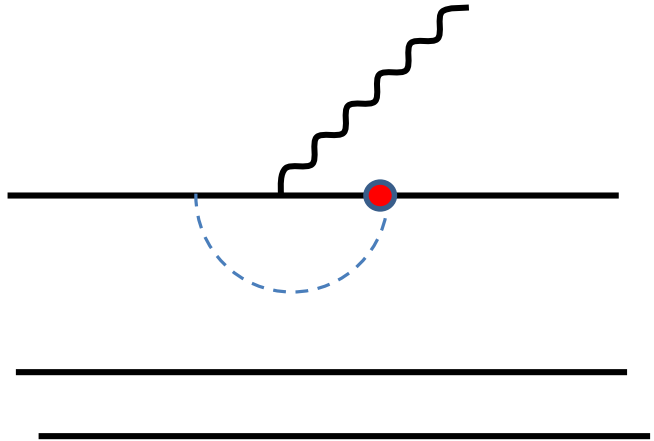
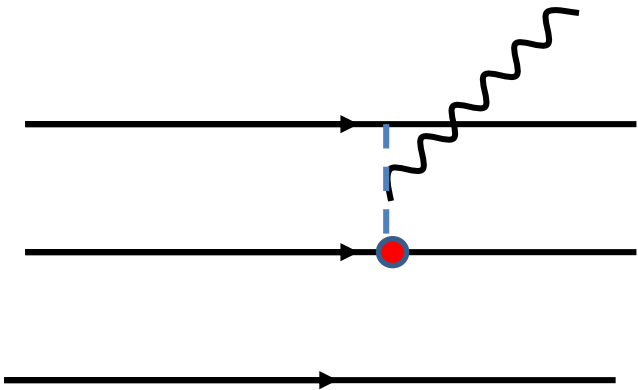
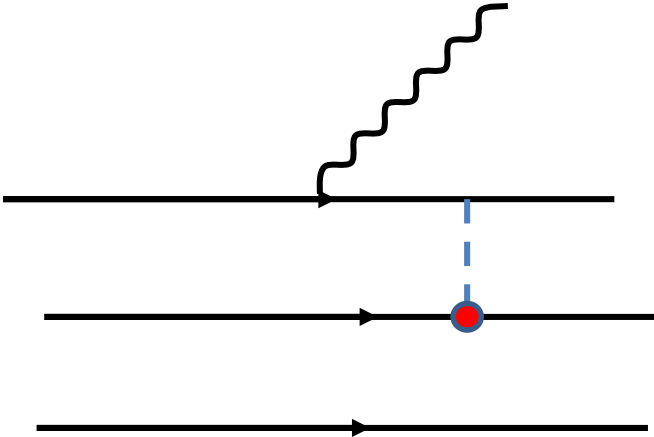
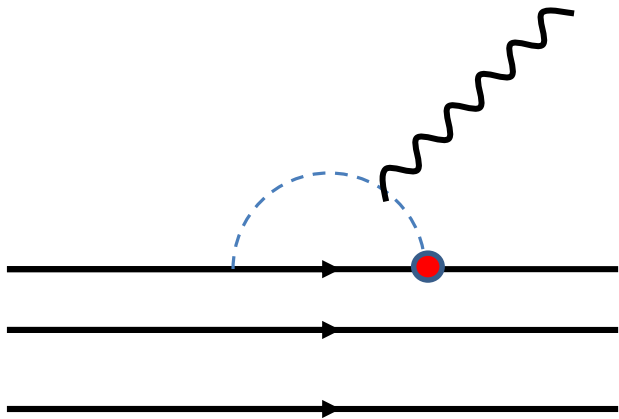
$$d_n = 0.14(\bar{g}_\pi^{(0)} - \bar{g}_\pi^{(2)}) - 0.02(\bar{g}_\rho^{(0)} - \bar{g}_\rho^{(1)} + 2\bar{g}_\rho^{(2)}) + 0.006(\bar{g}_\omega^{(0)} - \bar{g}_\omega^{(1)})$$

$$d_p = -0.08(\bar{g}_\pi^{(0)} - \bar{g}_\pi^{(2)}) + 0.03(\bar{g}_\pi^{(0)} + \bar{g}_\pi^{(1)} + 2\bar{g}_\pi^{(2)}) + 0.003(\bar{g}_\eta^{(0)} + \bar{g}_\eta^{(1)}) \\ + 0.02(\bar{g}_\rho^{(0)} + \bar{g}_\rho^{(1)} + 2\bar{g}_\rho^{(2)}) + 0.006(\bar{g}_\omega^{(0)} + \bar{g}_\omega^{(1)})$$

Meson exchange potentials for PV and TVPV interactions



Many Body system EDMs



${}^3\text{He}$ and ${}^3\text{H}$

$$\begin{aligned}d_{{}^3\text{He}} = & (-0.0542d_p + 0.868d_n) + 0.072[\bar{g}_\pi^{(0)} + 1.92\bar{g}_\pi^{(1)} \\ & + 1.21\bar{g}_\pi^{(2)} - 0.015\bar{g}_\eta^{(0)} + 0.03\bar{g}_\eta^{(1)} - 0.010\bar{g}_\rho^{(0)} \\ & + 0.015\bar{g}_\rho^{(1)} - 0.012\bar{g}_\rho^{(2)} + 0.021\bar{g}_\omega^{(0)} - 0.06\bar{g}_\omega^{(1)}] \text{efm}\end{aligned}$$

$$\begin{aligned}d_{{}^3\text{H}} = & (0.868d_p - 0.0552d_n) - 0.072[\bar{g}_\pi^{(0)} - 1.97\bar{g}_\pi^{(1)} \\ & + 1.26\bar{g}_\pi^{(2)} - 0.015\bar{g}_\eta^{(0)} - 0.030\bar{g}_\eta^{(1)} \\ & - 0.010\bar{g}_\rho^{(0)} - 0.015\bar{g}_\rho^{(1)} - 0.012\bar{g}_\rho^{(2)} \\ & + 0.022\bar{g}_\omega^{(0)} + 0.061\bar{g}_\omega^{(1)}] \text{efm}.\end{aligned}$$

Major Contributions

$$d_n \sim 0.14(\bar{g}_\pi^{(0)} - \bar{g}_\pi^{(2)})$$

$$d_p \sim 0.14\bar{g}_\pi^{(2)}$$

$$d_d \sim 0.22\bar{g}_\pi^{(1)}$$

$$d_{^3\text{He}} \sim 0.2\bar{g}_\pi^{(0)} + 0.14\bar{g}_\pi^{(1)}$$

$$d_{^3\text{H}} \sim 0.22\bar{g}_\pi^{(0)} - 0.14\bar{g}_\pi^{(1)}$$

$$P \sim \bar{g}_\pi^{(0)} + 0.3\bar{g}_\pi^{(1)}$$

Why neutron-nuclei?

- Search for TRIV & New Physics
independent test (for the case of suppression/cancelation)
- High Intensity Neutron Facilities
SNS in Oak Ridge, JSNS at J-PARC
- Nuclear Enhancement

Neutron transmission (= “EDM quality”)

P- and T-violation: $\vec{\sigma}_n \cdot [\vec{k} \times \vec{I}]$

P.K. Kabir, PR D25, (1982) 2013

L.. Stodolsky, N.P. B197 (1982) 213

T-violation: $(\vec{\sigma}_n \cdot [\vec{k} \times \vec{I}])(\vec{k} \cdot \vec{I})$

(for 5.9 MeV, on ^{165}Ho : $<1.2 \cdot 10^{-3}$, P. R. Huffman et al. , PRL 76, 4681 (1996))

P-violation: $(\vec{\sigma}_n \cdot \vec{k}) \sim 10^{-1}$ (not 10^{-7})

Enhanced of about 10^6

$$\Delta\sigma_v = \frac{4\pi}{k} \text{Im}\{\Delta f_v\}$$

$$\frac{d\psi}{dz} = \frac{2\pi N}{k} \text{Re}\{\Delta f_v\}$$

O. P. Sushkov and V. V. Flambaum, JETP Pisma 32 (1980) 377

V. E. Bunakov and V.G., Z. Phys. A303 (1981) 285

PV (First order effects)

$$f = f_{PC} + f_{PV}$$

$$W \sim |f_{PC} + f_{PV}|^2 = |f_{PC}|^2 + 2\Re(f_{PC}f_{PV}^*) + |f_{PV}|^2$$

$$\alpha \sim \frac{\Re(f_{PC}f_{PV}^*)}{|f_{PC}|^2} \sim \frac{|f_{PV}|}{|f_{PC}|}$$

$$\alpha \sim G_F m_\pi^2 \sim 2 \cdot 10^{-7}$$

T-Reversal Invariance

$$a + A \rightarrow b + B$$

$$a + A \leftarrow b + B$$

$$\vec{k}_{i,f} \rightarrow -\vec{k}_{f,i} \quad \text{and} \quad \vec{s} \rightarrow -\vec{s}$$

$$\langle \vec{k}_f, m_b, m_B | \hat{T} | \vec{k}_i, m_a, m_A \rangle = (-1)^{\sum_i s_i - m_i} \langle -\vec{k}_i, -m_a, -m_A | \hat{T} | -\vec{k}_f, -m_b, -m_B \rangle$$

Detailed Balance Principle (DBP):

$$\frac{(2s_a + 1)(2s_A + 1) k_i^2 (d\sigma / d\Omega)_{if}}{(2s_b + 1)(2s_B + 1) k_f^2 (d\sigma / d\Omega)_{fi}} = 1$$

FSI:

$$T^+ - T = iTT^+$$

in the first Born approximation T -is hermitian

$$\langle i | T | f \rangle = \langle i | T^* | f \rangle$$

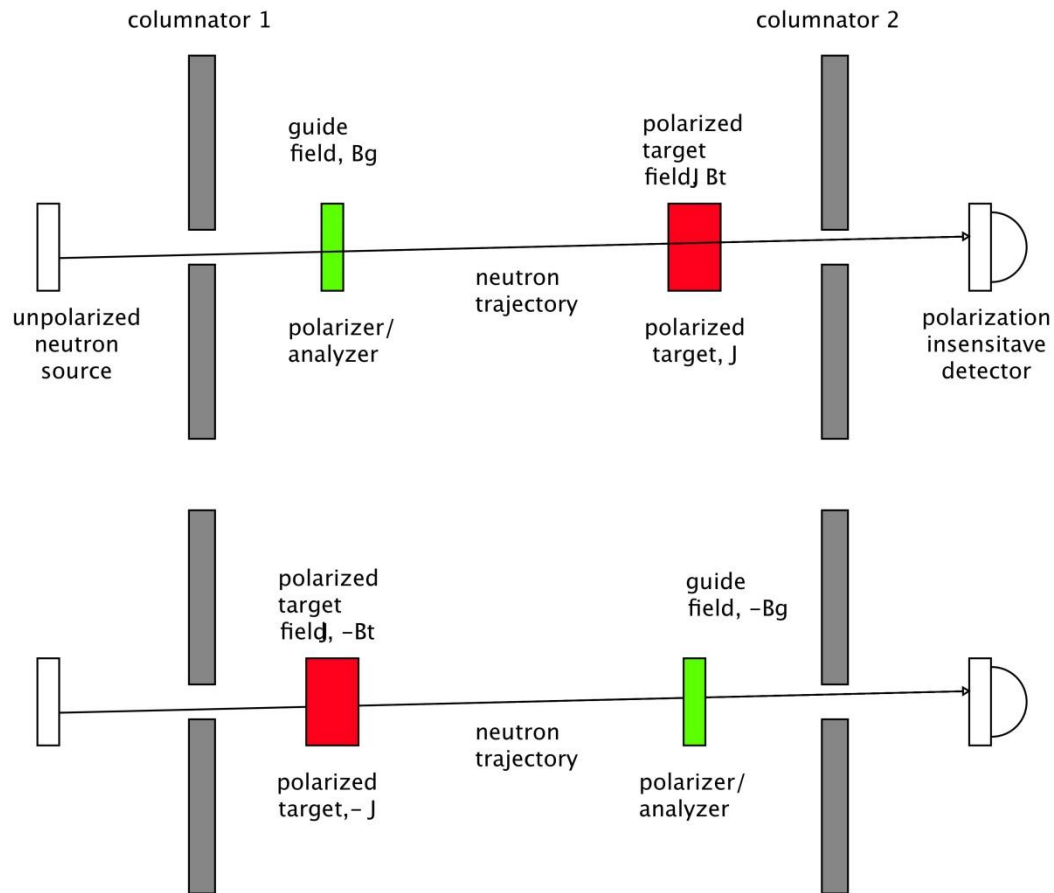
$$\begin{aligned} \oplus \text{ T-invariance} &\Rightarrow \langle f | T | i \rangle = \langle -f | T | -i \rangle^* \\ &\Rightarrow |\langle f | T | i \rangle|^2 = |\langle -f | T | -i \rangle|^2 \end{aligned}$$

then the probability is even function of time.

For an elastic scattering at the zero angle: " i " \equiv " f ",
then always "T-odd correlations" = "T-violation"

(R. M. Ryndin)

No Systematics



courtesy of J. D. Bowman

TRIV Transmission Theorem

$$H = a + b(\vec{\sigma} \cdot \vec{I}) + c(\vec{\sigma} \cdot \vec{k}) + d(\vec{\sigma} \cdot [\vec{k} \times \vec{I}])$$

$$U_F = \prod_{j=1}^m \exp\left(-i \frac{\Delta t_j}{\hbar} H_j^F\right) = \alpha + (\vec{\beta} \cdot \vec{\sigma})$$

$$U_R = \prod_{j=m}^1 \exp\left(-i \frac{\Delta t_j}{\hbar} H_j^R\right) = \alpha - (\vec{\beta} \cdot \vec{\sigma}).$$

$$T_F = \frac{1}{2} \text{Tr}(U_F^\dagger U_F) = \alpha^* \alpha + (\vec{\beta}^* \cdot \vec{\beta}) = \frac{1}{2} \text{Tr}(U_R^\dagger U_R) = T_R$$

Neutron transmission (= “EDM quality”)

P- and T-violation: $\vec{\sigma}_n \cdot [\vec{k} \times \vec{I}]$

P.K. Kabir, PR D25, (1982) 2013

L.. Stodolsky, N.P. B197 (1982) 213

P-violation: $(\vec{\sigma}_n \cdot \vec{k}) \sim 10^{-1}$ (*not* 10^{-7})

Enhanced of about 10^6

O. P. Sushkov and V. V. Flambaum, JETP Pisma 32 (1980) 377

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$$\Delta\sigma_v = \frac{4\pi}{k} \text{Im}\{\Delta f_v\}$$

$$\frac{d\psi}{dz} = \frac{2\pi N}{k} \text{Re}\{\Delta f_v\}$$

General formalism

$$2\pi i \hat{T} = \hat{1} - \hat{S} = \hat{R}$$

$$\vec{S} = \vec{s} + \vec{I} \quad \text{and} \quad \vec{J} = \vec{l} + \vec{S}$$

$$2\pi i \langle \vec{k} \mu | T | \vec{k} \mu \rangle = \sum_{JMlm'l'm'_s Sm_s S'm'_s} Y_{l'm'}(\theta, \phi) \langle s\mu IM_I | S'm'_s \rangle \langle l'm' S'm'_s | JM \rangle \\ \times \langle S'l'\alpha' | R^J | Sl\alpha \rangle \langle JM | lmSm_s \rangle \langle Sm_s | s\mu IM_I \rangle Y_{lm}^*(\theta, \phi)$$

DWBA

$$T_{if} = \langle \Psi_f^- | W | \Psi_i^+ \rangle$$

$$\Psi_{i,f}^\pm = \sum_k a_{k(i,f)}^\pm(E) \phi_k + \sum_m \int b_{m(i,f)}^\pm(E, E') \chi_m^\pm(E') dE'$$

$$a_{k(i,f)}^\pm(E) = \frac{\exp(\pm i\delta_{i,f})}{\sqrt{2\pi}} \frac{(\Gamma_k^{i,f})^{1/2}}{E - E_k \pm i\Gamma_k / 2}$$

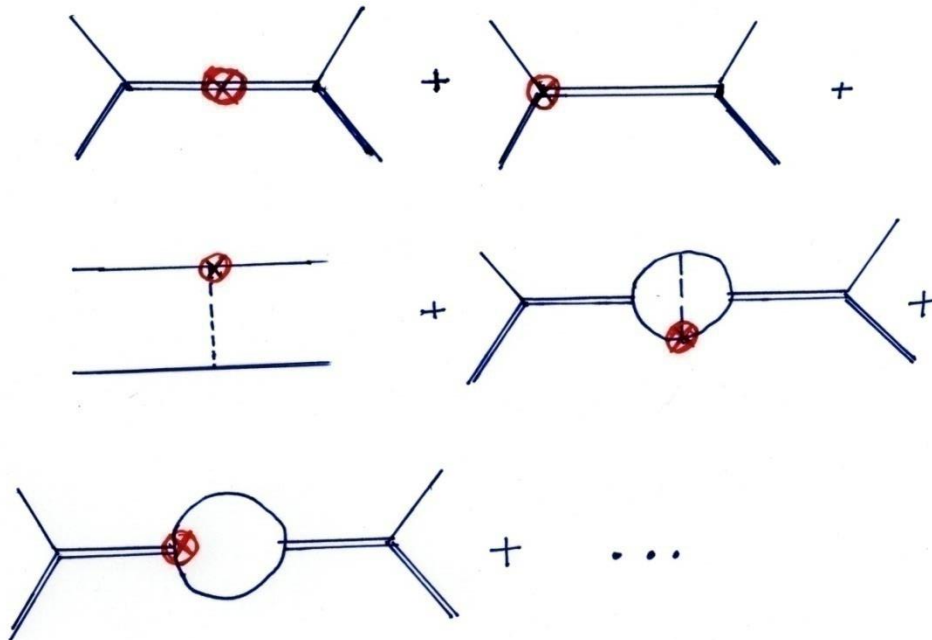
$$(\Gamma_k^i)^{1/2} = \sqrt{2\pi} \langle \chi_i(E') | V | \phi_k \rangle$$

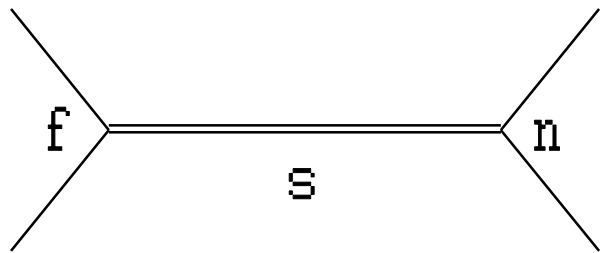
$$b_{m,\alpha}^\pm(E, E') = \exp(\pm i\delta_\alpha) \delta(E - E') + a_{k,\alpha}^\pm \frac{\langle \phi_k | V | \chi_m(E') \rangle}{E - E' \pm i\varepsilon}$$

$$\Gamma / D \ll 1 \Rightarrow$$

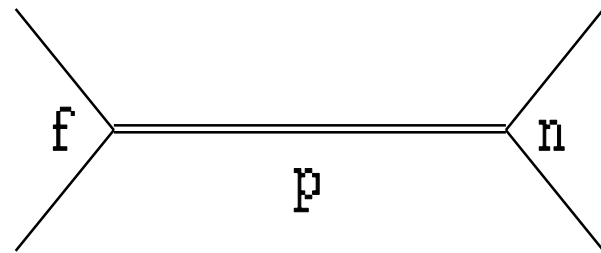
$$T_{PV} = a_{s,i}^+ a_{p,f}^+ \langle \phi_p | W | \phi_s \rangle + a_{s,i}^+ e^{i\delta_p^f} \langle \chi_{p,f}^+ | W | \phi_s \rangle +$$

$$+ e^{i(\delta_s^i + \delta_p^f)} \langle \chi_{p,f}^+ | W | \chi_{s,i} \rangle + \dots$$





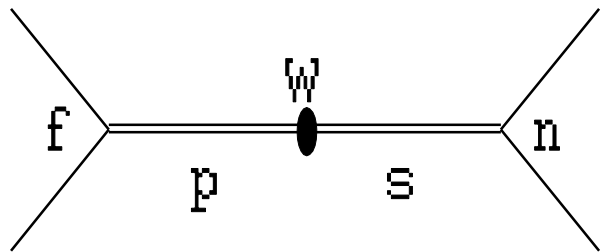
s



p

\mathcal{L}

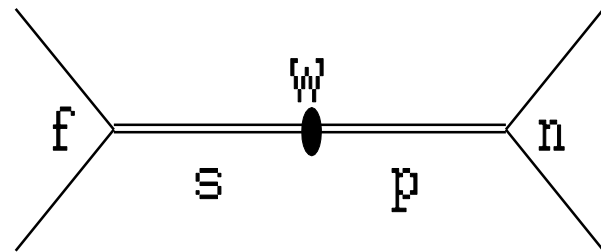
\mathcal{L}



p

s

\mathcal{L}



s

p

\mathcal{L}

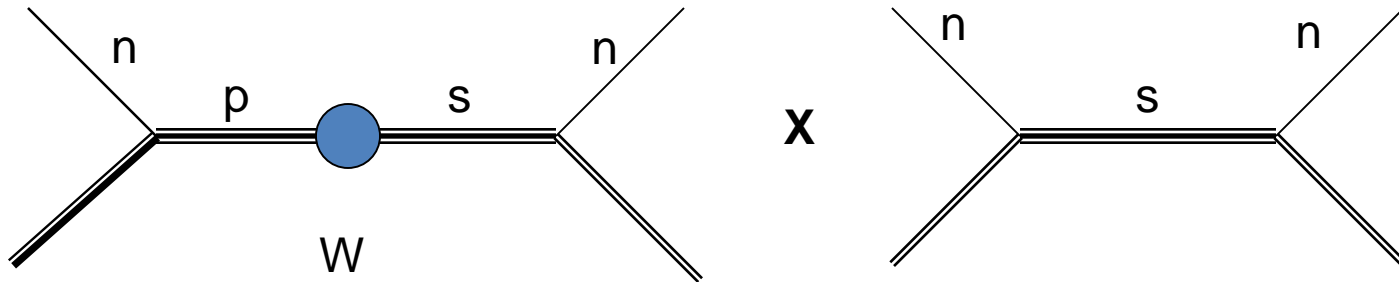
General Expressions

$$\Delta f_{TP} = m \frac{\sqrt{3}I}{8\pi k \sqrt{2I+1}} \left(\frac{\langle (I-1/2), 0 | R^{I-1/2} | (I+1/2), 1 \rangle - \langle (I+1/2), 1 | R^{I-1/2} | (I-1/2), 0 \rangle}{\sqrt{I+1}} + \frac{\langle (I+1/2), 0 | R^{I+1/2} | (I-1/2), 1 \rangle - \langle (I-1/2), 1 | R^{I+1/2} | (I+1/2), 0 \rangle}{\sqrt{I}} \right)$$

$$\langle S' s | R^J | S p \rangle = \frac{\sqrt{\Gamma_s^n(S')} (-i\mathbf{v} + \mathbf{w}) \sqrt{\Gamma_p^n(S)}}{(E - E_s + i\Gamma_s / 2)(E - E_p + i\Gamma_p / 2)} e^{i(\delta_s(S') + \delta_p(S))}$$

$$\int \varphi_s W \varphi_p d\tau = -\mathbf{v} - i\mathbf{w}$$

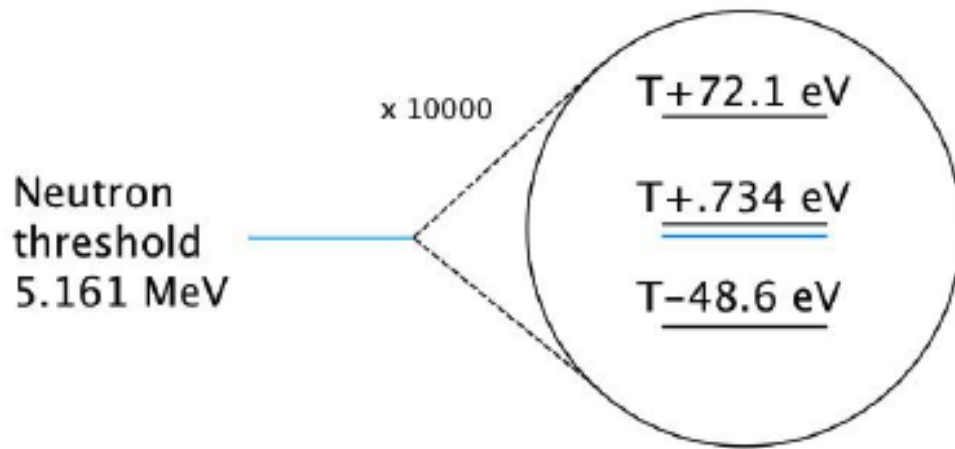
P- and T-violation in a **Relative** measurement!!! & Enhancements



$$\Delta\sigma_T \sim \vec{\sigma}_n \cdot [\vec{k} \times \vec{I}] \sim \frac{W \sqrt{\Gamma_s^n \Gamma_p^n(s)}}{(E - E_s + i\Gamma_s/2)(E - E_p + i\Gamma_p/2)} [(E - E_s)\Gamma_p + (E - E_p)\Gamma_s]$$

$$\Delta\sigma_T / \Delta\sigma_P \sim \lambda = \frac{g_T}{g_P} \quad [\sim - ?]$$

$^{139}\text{La}+n$ System



Compound-Nuclear
States in $^{139}\text{La}+n$
system

140La G. S.

courtesy of J. D. Bowman

TVPV n-D

$$\vec{\sigma}_n \cdot [\vec{k} \times \vec{I}]$$

$$P^{T\dot{\Phi}} = \frac{\Delta\sigma^{T\dot{\Phi}}}{2\sigma_{tot}} = \frac{(-0.185 \text{ b})}{2\sigma_{tot}} [\bar{g}_\pi^{(0)} + 0.26\bar{g}_\pi^{(1)} - 0.0012\bar{g}_\eta^{(0)} + 0.0034\bar{g}_\eta^{(1)} - 0.0071\bar{g}_\rho^{(0)} + 0.0035\bar{g}_\rho^{(1)} + 0.0019\bar{g}_\omega^{(0)} - 0.00063\bar{g}_\omega^{(1)}]$$

$$P^{\dot{\Phi}} = \frac{\Delta\sigma^{\dot{\Phi}}}{2\sigma_{tot}} = \frac{(0.395 \text{ b})}{2\sigma_{tot}} [h_\pi^1 + h_\rho^0(0.021) + h_\rho^1(0.0027) + h_\omega^0(0.022) + h_\omega^1(-0.043) + h_\rho'^1(-0.012)]$$

$$\frac{\Delta\sigma^{T\dot{\Phi}}}{\Delta\sigma^{\dot{\Phi}}} \simeq (-0.47) \left(\frac{\bar{g}_\pi^{(0)}}{h_\pi^1} + (0.26) \frac{\bar{g}_\pi^{(1)}}{h_\pi^1} \right)$$

- Y.-H. Song, R. Lazauskas and V. G., Phys. Rev. C83, 065503 (2011).

Enhancements:

- “Weak” structure

$$\frac{\Delta\sigma^{TP}}{\Delta\sigma^P} \sim \left(\frac{\bar{g}_\pi^{(0)}}{h_\pi^1} + (0.26) \frac{\bar{g}_\pi^{(1)}}{h_\pi^1} \right)$$

$h_\pi^1 \sim 4.6 \cdot 10^{-7}$ "best" DDH
or 10 - 100 Enhancement!!!

- “Strong” structure

P-violation:

$$(\vec{\sigma}_n \cdot \vec{k}) \sim 10^{-1} \text{ (not } 10^{-7} \text{)}$$

Enhanced of about $\sim 10^6$

O. P. Sushkov and V. V. Flambaum, JETP Pisma 32 (1980) 377

V. E. Bunakov and V.G., Z. Phys. A303 (1981) 285

Large N_C expansion

Hierarchy of couplings:

$$\bar{g}_\pi^{(1)} \sim N_C^{1/2} > \bar{g}_\pi^{(0)} \sim \bar{g}_\pi^{(2)} \sim N_C^{-1/2}$$

$$h_\pi^{(1)} \sim N_C^{-1/2}$$

Strong-interaction **enhancement** of TVPV
compared to PV one-pion exchange

EDM limits

From n EDM ⁽¹⁾

$$\bar{g}_{\pi}^{(0)} < 2.5 \cdot 10^{-10}$$

From ^{199}Hg EDM ⁽²⁾

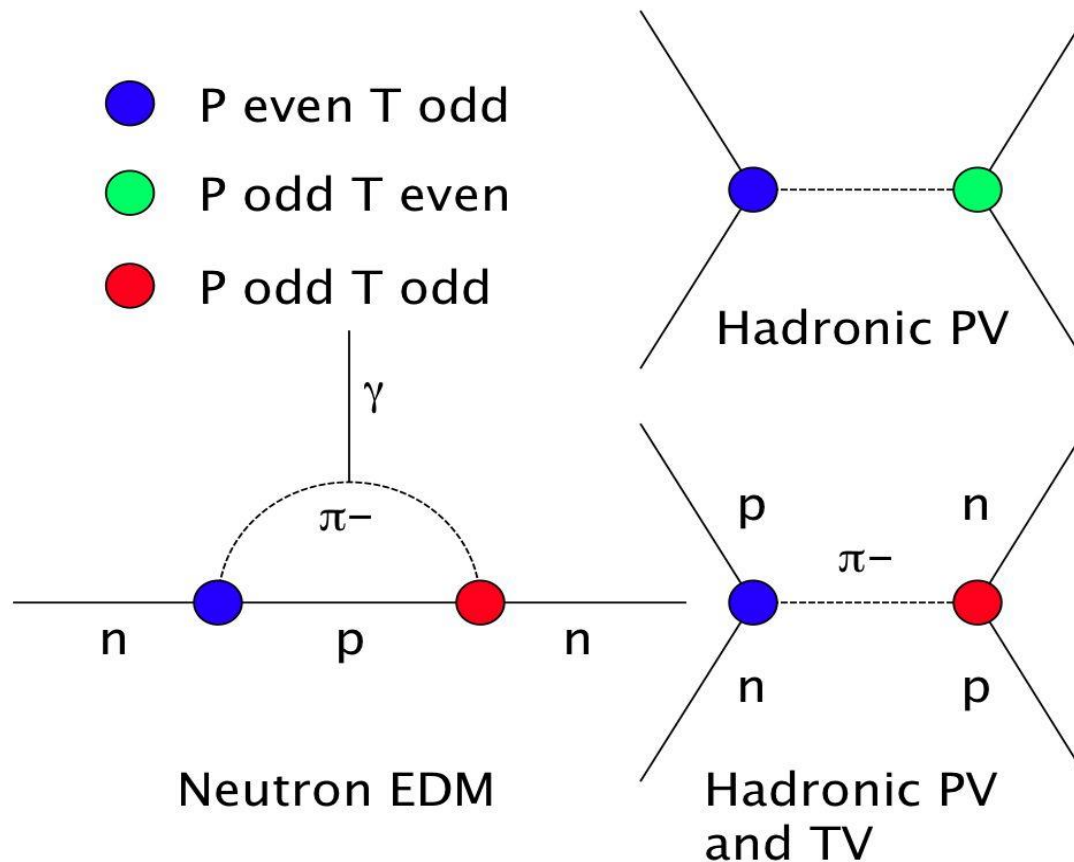
$$\bar{g}_{\pi}^{(1)} < 0.5 \cdot 10^{-10}$$

$\Rightarrow \frac{\cancel{TP}}{\cancel{P}} \sim 10^{-3}$ from the current EDMs

\equiv "discovery potential" 10^2 (nucl) -- 10^4 (nucl & "weak")

- M. Pospelov and A. Ritz (2005)
- V. Dmitriev and I. Khriplovich (2004)

Meson exchange potentials for PV and TVPV interactions



TVPV potential

P. Herczeg (1966)

$$\begin{aligned}
 V_{T\hat{P}} = & \left[-\frac{\bar{g}_\eta^{(0)} g_\eta m_\eta^2}{2m_N 4\pi} Y_1(x_\eta) + \frac{\bar{g}_\omega^{(0)} g_\omega m_\omega^2}{2m_N 4\pi} Y_1(x_\omega) \right] \sigma_- \cdot \hat{r} \\
 & + \left[-\frac{\bar{g}_\pi^{(0)} g_\pi m_\pi^2}{2m_N 4\pi} Y_1(x_\pi) + \frac{\bar{g}_\rho^{(0)} g_\rho m_\rho^2}{2m_N 4\pi} Y_1(x_\rho) \right] \tau_1 \cdot \tau_2 \sigma_- \cdot \hat{r} \\
 & + \left[-\frac{\bar{g}_\pi^{(2)} g_\pi m_\pi^2}{2m_N 4\pi} Y_1(x_\pi) + \frac{\bar{g}_\rho^{(2)} g_\rho m_\rho^2}{2m_N 4\pi} Y_1(x_\rho) \right] T_{12}^z \sigma_- \cdot \hat{r} \\
 & + \left[-\frac{\bar{g}_\pi^{(1)} g_\pi m_\pi^2}{4m_N 4\pi} Y_1(x_\pi) + \frac{\bar{g}_\eta^{(1)} g_\eta m_\eta^2}{4m_N 4\pi} Y_1(x_\eta) + \frac{\bar{g}_\rho^{(1)} g_\rho m_\rho^2}{4m_N 4\pi} Y_1(x_\rho) + \frac{\bar{g}_\omega^{(1)} g_\omega m_\omega^2}{2m_N 4\pi} Y_1(x_\omega) \right] \tau_+ \sigma_- \cdot \hat{r} \\
 & + \left[-\frac{\bar{g}_\pi^{(1)} g_\pi m_\pi^2}{4m_N 4\pi} Y_1(x_\pi) - \frac{\bar{g}_\eta^{(1)} g_\eta m_\eta^2}{4m_N 4\pi} Y_1(x_\eta) - \frac{\bar{g}_\rho^{(1)} g_\rho m_\rho^2}{4m_N 4\pi} Y_1(x_\rho) + \frac{\bar{g}_\omega^{(1)} g_\omega m_\omega^2}{2m_N 4\pi} Y_1(x_\omega) \right] \tau_- \sigma_+ \cdot \hat{r}
 \end{aligned}$$

- Y.-H. Song, R. Lazauskas and V. G, Phys. Rev. C83, 065503 (2011).

PV nucleon Potential

$$\begin{aligned}
 V_{\text{DDH}}^{\text{PV}}(\vec{r}) = & i \frac{h_{\pi}^1 g_A m_N}{\sqrt{2} F_{\pi}} \left(\frac{\tau_1 \times \tau_2}{2} \right)_3 (\vec{\sigma}_1 + \vec{\sigma}_2) \cdot \left[\frac{\vec{p}_1 - \vec{p}_2}{2m_N}, w_{\pi}(r) \right] \\
 & - g_{\rho} \left(h_{\rho}^0 \tau_1 \cdot \tau_2 + h_{\rho}^1 \left(\frac{\tau_1 + \tau_2}{2} \right)_3 + h_{\rho}^2 \frac{(3\tau_1^3 \tau_2^3 - \tau_1 \cdot \tau_2)}{2\sqrt{6}} \right) \\
 & \times \left((\vec{\sigma}_1 - \vec{\sigma}_2) \cdot \left\{ \frac{\vec{p}_1 - \vec{p}_2}{2m_N}, w_{\rho}(r) \right\} \right. \\
 & \left. + i(1 + \chi_{\rho}) \vec{\sigma}_1 \times \vec{\sigma}_2 \cdot \left[\frac{\vec{p}_1 - \vec{p}_2}{2m_N}, w_{\rho}(r) \right] \right) \\
 & - g_{\omega} \left(h_{\omega}^0 + h_{\omega}^1 \left(\frac{\tau_1 + \tau_2}{2} \right)_3 \right) \\
 & \times \left((\vec{\sigma}_1 - \vec{\sigma}_2) \cdot \left\{ \frac{\vec{p}_1 - \vec{p}_2}{2m_N}, w_{\omega}(r) \right\} \right. \\
 & \left. + i(1 + \chi_{\omega}) \vec{\sigma}_1 \times \vec{\sigma}_2 \cdot \left[\frac{\vec{p}_1 - \vec{p}_2}{2m_N}, w_{\omega}(r) \right] \right) \\
 & - \left(g_{\omega} h_{\omega}^1 - g_{\rho} h_{\rho}^1 \right) \left(\frac{\tau_1 - \tau_2}{2} \right)_3 (\vec{\sigma}_1 + \vec{\sigma}_2) \cdot \left\{ \frac{\vec{p}_1 - \vec{p}_2}{2m_N}, w_{\rho}(r) \right\} \\
 & - g_{\rho} h_{\rho}^1 i \left(\frac{\tau_1 \times \tau_2}{2} \right)_3 (\vec{\sigma}_1 + \vec{\sigma}_2) \cdot \left[\frac{\vec{p}_1 - \vec{p}_2}{2m_N}, w_{\rho}(r) \right].
 \end{aligned}$$

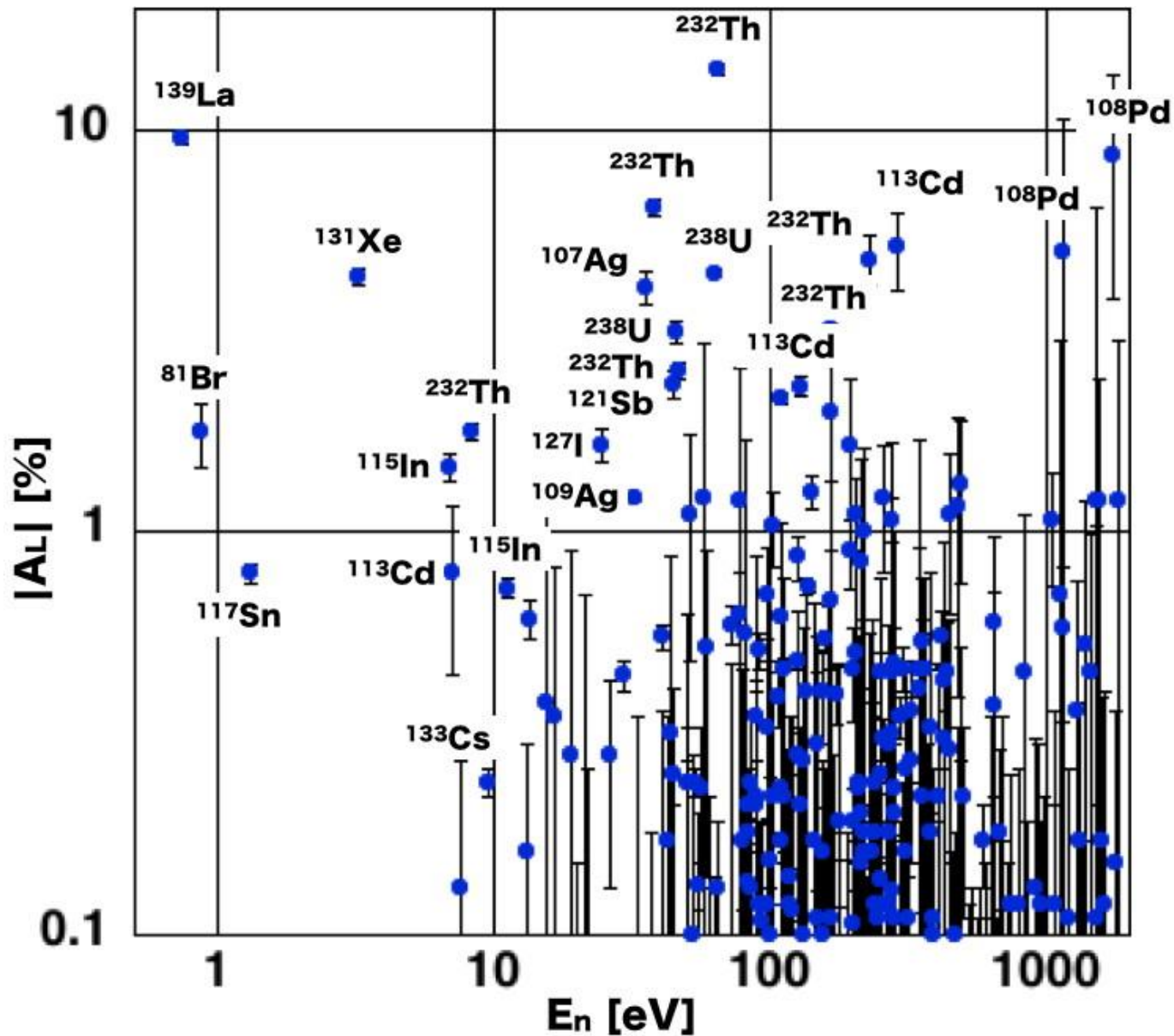
PV nucleon Potential

| n | c_n^{DDH} | $f_n^{\text{DDH}}(r)$ | $c_n^{\mathcal{I}}$ | $f_n^{\mathcal{I}}(r)$ | c_n^{π} | $f_n^{\pi}(r)$ | $O_{ij}^{(n)}$ |
|-----|---|-----------------------|---|----------------------------|--|--------------------------|--|
| 1 | $+\frac{g_{\pi}}{2\sqrt{2}m_N}h_{\pi}^1$ | $f_{\pi}(r)$ | $\frac{2\mu^2}{\Lambda_{\chi}^3}C_6^{\mathcal{I}}$ | $f_{\mu}^{\mathcal{I}}(r)$ | $+\frac{g_{\pi}}{2\sqrt{2}m_N}h_{\pi}^1$ | $f_{\pi}(r)$ | $(\tau_i \times \tau_j)^z(\sigma_i + \sigma_j) \cdot X_{ij,-}^{(1)}$ |
| 2 | $-\frac{g_{\rho}}{m_N}h_{\rho}^0$ | $f_{\rho}(r)$ | 0 | 0 | 0 | 0 | $(\tau_i \cdot \tau_j)(\sigma_i - \sigma_j) \cdot X_{ij,+}^{(2)}$ |
| 3 | $-\frac{g_{\rho}(1+\kappa_{\rho})}{m_N}h_{\rho}^0$ | $f_{\rho}(r)$ | 0 | 0 | 0 | 0 | $(\tau_i \cdot \tau_j)(\sigma_i \times \sigma_j) \cdot X_{ij,-}^{(3)}$ |
| 4 | $-\frac{g_{\rho}}{2m_N}h_{\rho}^1$ | $f_{\rho}(r)$ | $\frac{\mu^2}{\Lambda_{\chi}^3}(C_2^{\mathcal{I}} + C_4^{\mathcal{I}})$ | $f_{\mu}^{\mathcal{I}}(r)$ | $\frac{\Lambda^2}{\Lambda_{\chi}^3}(C_2^{\pi} + C_4^{\pi})$ | $f_{\Lambda}(r)$ | $(\tau_i + \tau_j)^z(\sigma_i - \sigma_j) \cdot X_{ij,+}^{(4)}$ |
| 5 | $-\frac{g_{\rho}(1+\kappa_{\rho})}{2m_N}h_{\rho}^1$ | $f_{\rho}(r)$ | 0 | 0 | $\frac{2\sqrt{2}\pi g_A^3 \Lambda^2}{\Lambda_{\chi}^3}h_{\pi}^1$ | $L_{\Lambda}(r)$ | $(\tau_i + \tau_j)^z(\sigma_i \times \sigma_j) \cdot X_{ij,-}^{(5)}$ |
| 6 | $-\frac{g_{\rho}}{2\sqrt{6}m_N}h_{\rho}^2$ | $f_{\rho}(r)$ | $-\frac{2\mu^2}{\Lambda_{\chi}^3}C_5^{\mathcal{I}}$ | $f_{\mu}^{\mathcal{I}}(r)$ | $-\frac{2\Lambda^2}{\Lambda_{\chi}^3}C_5^{\pi}$ | $f_{\Lambda}(r)$ | $\mathcal{T}_{ij}(\sigma_i - \sigma_j) \cdot X_{ij,+}^{(6)}$ |
| 7 | $-\frac{g_{\rho}(1+\kappa_{\rho})}{2\sqrt{6}m_N}h_{\rho}^2$ | $f_{\rho}(r)$ | 0 | 0 | 0 | 0 | $\mathcal{T}_{ij}(\sigma_i \times \sigma_j) \cdot X_{ij,-}^{(7)}$ |
| 8 | $-\frac{g_{\omega}}{m_N}h_{\omega}^0$ | $f_{\omega}(r)$ | $\frac{2\mu^2}{\Lambda_{\chi}^3}C_1^{\mathcal{I}}$ | $f_{\mu}^{\mathcal{I}}(r)$ | $\frac{2\Lambda^2}{\Lambda_{\chi}^3}C_1^{\pi}$ | $f_{\Lambda}(r)$ | $(\sigma_i - \sigma_j) \cdot X_{ij,+}^{(8)}$ |
| 9 | $-\frac{g_{\omega}(1+\kappa_{\omega})}{m_N}h_{\omega}^0$ | $f_{\omega}(r)$ | $\frac{2\mu^2}{\Lambda_{\chi}^3}\tilde{C}_1^{\mathcal{I}}$ | $f_{\mu}^{\mathcal{I}}(r)$ | $\frac{2\Lambda^2}{\Lambda_{\chi}^3}\tilde{C}_1^{\pi}$ | $f_{\Lambda}(r)$ | $(\sigma_i \times \sigma_j) \cdot X_{ij,-}^{(9)}$ |
| 10 | $-\frac{g_{\omega}}{2m_N}h_{\omega}^1$ | $f_{\omega}(r)$ | 0 | 0 | 0 | 0 | $(\tau_i + \tau_j)^z(\sigma_i - \sigma_j) \cdot X_{ij,+}^{(10)}$ |
| 11 | $-\frac{g_{\omega}(1+\kappa_{\omega})}{2m_N}h_{\omega}^1$ | $f_{\omega}(r)$ | 0 | 0 | 0 | 0 | $(\tau_i + \tau_j)^z(\sigma_i \times \sigma_j) \cdot X_{ij,-}^{(11)}$ |
| 12 | $-\frac{g_{\omega}h_{\omega}^1 - g_{\rho}h_{\rho}^1}{2m_N}$ | $f_{\rho}(r)$ | 0 | 0 | 0 | 0 | $(\tau_i - \tau_j)^z(\sigma_i + \sigma_j) \cdot X_{ij,+}^{(12)}$ |
| 13 | $-\frac{g_{\rho}}{2m_N}h_{\rho}^1$ | $f_{\rho}(r)$ | 0 | 0 | $-\frac{\sqrt{2}\pi g_A \Lambda^2}{\Lambda_{\chi}^3}h_{\pi}^1$ | $L_{\Lambda}(r)$ | $(\tau_i \times \tau_j)^z(\sigma_i + \sigma_j) \cdot X_{ij,-}^{(13)}$ |
| 14 | 0 | 0 | 0 | 0 | $\frac{2\Lambda^2}{\Lambda_{\chi}^3}C_6^{\pi}$ | $f_{\Lambda}(r)$ | $(\tau_i \times \tau_j)^z(\sigma_i + \sigma_j) \cdot X_{ij,-}^{(14)}$ |
| 15 | 0 | 0 | 0 | 0 | $\frac{\sqrt{2}\pi g_A^3 \Lambda^2}{\Lambda_{\chi}^3}h_{\pi}^1$ | $\tilde{L}_{\Lambda}(r)$ | $(\tau_i \times \tau_j)^z(\sigma_i + \sigma_j) \cdot X_{ij,-}^{(15)}$ |

$$V_{ij} = \sum_{\alpha} c_n^{\alpha} O_{ij}^{(n)};$$

$$X_{ij,+}^{(n)} = [\vec{p}_{ij}, f_n(r_{ij})]_{+} \rightarrow X_{ij,-}^{(n)} = i[\vec{p}_{ij}, f_n(r_{ij})]_{-} \quad 33$$

- TVPV interactions are “simpler” than PV ones
- All TVPV operators are presented in PV potential
- If one can calculate PV effects, TVPV can be calculated with even better accuracy



G.E. MITCHELL, J.D. BOWMAN, S.I. PENTTILAG , E.I. SHARAPOV, Phys. Rep. 354 (2001) 157

Conclusions

- No FSI = like “EDM”
- Relative values → cancelations of “unknowns”
- Reasonably simple theoretical description
- A possibility for an additional **enhancement**
- Sensitive to **a variety of TRIV** couplings
- New facilities with high neutron fluxes



The possibility to improve limits on **TRIV**
(or to discover **new physics**) by $10^2 - 10^4$
at SNS ORNL and JSNS J-PARC

Thank you!

Extra Slides:

Statistical theory of parity nonconservation in compound nuclei

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Comparison of experimental CN matrix elements with Tomsovic theory using DDH “best” meson-nucleon couplings: agreement within a factor of 2

TABLE IV. Theoretical values of M for the effective parity-violating interaction. Contributions are shown separately for the standard (Std) and doorway (Dwy) pieces of the two-body interaction. A comparison of the experimental value of M given in Table III is also shown.

| Nucleus | M_{Std} (meV) | M_{Dwy} (meV) | $M_{Std+Dwy}$ (meV) | M_{expt} (meV) |
|-------------------|-----------------|-----------------|---------------------|------------------------|
| ^{239}U | 0.116 | 0.177 | 0.218 | $0.67^{+0.24}_{-0.16}$ |
| ^{105}Pd | 0.70 | 0.79 | 1.03 | $2.2^{+2.4}_{-0.9}$ |
| ^{106}Pd | 0.304 | 0.357 | 0.44 | $0.20^{+0.10}_{-0.07}$ |
| ^{107}Pd | 0.698 | 0.728 | 0.968 | $0.79^{+0.88}_{-0.36}$ |
| ^{109}Pd | 0.73 | 0.72 | 0.97 | $1.6^{+2.0}_{-0.7}$ 39 |

$$-i \frac{\langle a' | V^{P,T} | a \rangle}{\langle a' | V^P | a \rangle} = \kappa^{(1)} \frac{\bar{g}_{\pi NN}^{(1)'}}{g_{\rho NN}^{(0)'}}$$

TABLE II. Isovector π -exchange, $V_{P,T}$, and isoscalar ρ -exchange, V_P , matrix elements evaluated for a closed-shell-plus-one configuration for six choices of the closed-shell core. The weak interaction coupling constants are $\bar{g}_{\pi NN}^{(1)'} = 1.0 \times 10^{-11}$ and $g_{\rho NN}^{(0)'} = -11.4 \times 10^{-7}$. Matrix elements were calculated with harmonic oscillator wave functions with $\hbar\omega = 45A^{-1/3} - 25A^{-2/3}$ MeV. The Miller-Spencer [14] short-range correlation function was used. The ratio, $\kappa^{(1)}$, is defined in Eq. (6).

| | ¹⁶ O N=8 Z=8 | ⁴⁰ Ca N=20 Z=20 | ⁹⁰ Zr N=50 Z=40 | ¹³⁸ Ba N=82 Z=56 | ²⁰⁸ Pb N=126 Z=82 | ²³² Th N=142 Z=90 |
|---|-------------------------------|----------------------------------|----------------------------------|-----------------------------------|------------------------------------|------------------------------------|
| | <u>0p-0s</u> | <u>1p-1s</u> | <u>2p-2s</u> | <u>2p-2s</u> | <u>3p-3s</u> | <u>3p-3s</u> |
| $\langle V_{P,T} \rangle$ in 10^{-4} eV | 1.084 | 0.875 | 0.708 | 0.779 | 0.608 | 0.633 |
| $i\langle V_P \rangle$ in eV | 1.513 | 1.550 | 1.535 | 1.576 | 1.581 | 1.600 |
| $\kappa^{(1)}$ | -8.2 | -6.4 | -5.3 | -5.6 | -4.4 | -4.5 |
| | <u>0p-1s</u> | <u>1p-2s</u> | <u>2p-3s</u> | <u>2p-3s</u> | <u>3p-4s</u> | <u>3p-4s</u> |
| $\langle V_{P,T} \rangle$ in 10^{-4} eV | -0.400 | -0.378 | -0.388 | -0.465 | -0.376 | -0.409 |
| $i\langle V_P \rangle$ in eV | 1.294 | 1.435 | 1.441 | 1.485 | 1.508 | 1.527 |
| $\kappa^{(1)}$ | 3.5 | 3.0 | 3.1 | 3.6 | 2.8 | 3.0 |

Theoretical predictions

| Model | λ |
|---|-------------------------|
| Kobayashi – Maskawa | $\leq 10^{-10}$ |
| Right – Left | $\leq 4 \times 10^{-3}$ |
| Horizontal Symmetry | $\leq 10^{-5}$ |
| Weinberg (charged Higgs bosons) | $\leq 2 \times 10^{-6}$ |
| Weinberg (neutral Higgs bosons) | $\leq 3 \times 10^{-4}$ |
| θ -term in QCD Lagrangian | $\leq 5 \times 10^{-5}$ |
| Neutron EDM (one π -loop mechanism) | $\leq 4 \times 10^{-3}$ |
| Atomic EDM (^{199}Hg) | $\leq 2 \times 10^{-3}$ |

$$\lambda = \frac{g_{CP}}{g_P} \quad g_P = ??? \quad \Rightarrow \quad n+p \rightarrow d + \gamma$$

Ranking

$\bar{g}_\pi^{(0)} : \Rightarrow \text{Scattering, } ^3\text{He, } n$

$\bar{g}_\pi^{(1)} : \Rightarrow \text{Scattering, } D, ^3\text{He}$

Dominant

$\bar{g}_\pi^{(2)} : \Rightarrow ^3\text{H, } p, n$

$\bar{g}_\eta^{(0)} : \Rightarrow p, D$

$\bar{g}_\eta^{(1)} : \Rightarrow D, \text{Scattering}$

$\bar{g}_\rho^{(0)} : \Rightarrow n, p, ^3\text{He, } ^3\text{H}$

Sub-Dominant

$\bar{g}_\rho^{(1)} : \Rightarrow D, n, p$

$\bar{g}_\rho^{(2)} : \Rightarrow n, p, ^3\text{He, } ^3\text{H}$

$\bar{g}_\omega^{(0)} : \Rightarrow D$

$\bar{g}_\omega^{(1)} : \Rightarrow ^3\text{H, } n, p, \text{Scattering}$

Sensitivities (0-1)

